



# Application of ANFIS Technique for Wide-Band Modeling of Overvoltage of Single-Conductor Overhead Lines with Arrester above Dispersive and Two-Layer Soils

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**ABSTRACT:** In this paper, an efficient closed-form expression for overvoltage of overhead lines under direct strike in the presence of lightning arresters is presented. The lightning arresters are also grounded via two grounding systems namely vertical electrode and horizontal grid. The simulation results based on the exact method show that among different parameters, the resistivity of soil and line height affect the overvoltage. To extract the closed-form expression, adaptive-network-based fuzzy inference systems (ANFIS) are used. In creating the ANFIS-based expression, it is first assumed that the electrical parameters of the soil are constant. Then a number of input-output pairs (inputs are soil resistivity and line height and the output is overvoltage) are computed from exact methods to train the algorithm. Once the algorithm is converged, the efficient expression is extracted. This simple expression can be easily used in dispersive soils (frequency-variant electrical parameters) and horizontally two-layered soils (non-homogenous electrical parameters) provided that the equivalent frequency and equivalent resistivity concepts respectively in dispersive and two-layer soils are used.

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## 1- Introduction

Overvoltage of overhead lines subject to lightning strokes is a leading cause of short circuits and line outages in transmission systems [1]. Its computation is of importance due to its application in the insulation coordination study of power systems and the selection of respective lightning arresters. However, it is generally a difficult task because of the impulse characteristics of grounding systems and the nonlinear behavior of the arresters.

There are several approaches either in the frequency domain [2-4] or in the time domain [5-7]. The frequency-domain methods can easily incorporate the frequency dependence of electrical parameters of soil (dispersive soil) [3]. The time domain methods, on the other hand, are capable of treating nonlinear elements [6, 7]. However, they are inappropriate in including the dispersion of lossy soils. All mentioned methods suffer from time-consuming computations especially when the weather conditions are changed. To this end, a hybrid approach based on combining the Baum–Liu–Tesché (BLT) equations and the arithmetic operator method (AOM) has been proposed [8]. Since the BLT equations are based on the transmission line (TL) approximation, it is thus restricted to conditions at which  $kh \ll 1$  ( $k$  is wave number and  $h$  is the transmission line-height) [9], elsewhere it yields to violated results. It means that it is acceptable for slow-fronted currents containing lower frequency content with respect to fast-fronted currents, or low-valued heights. Also,

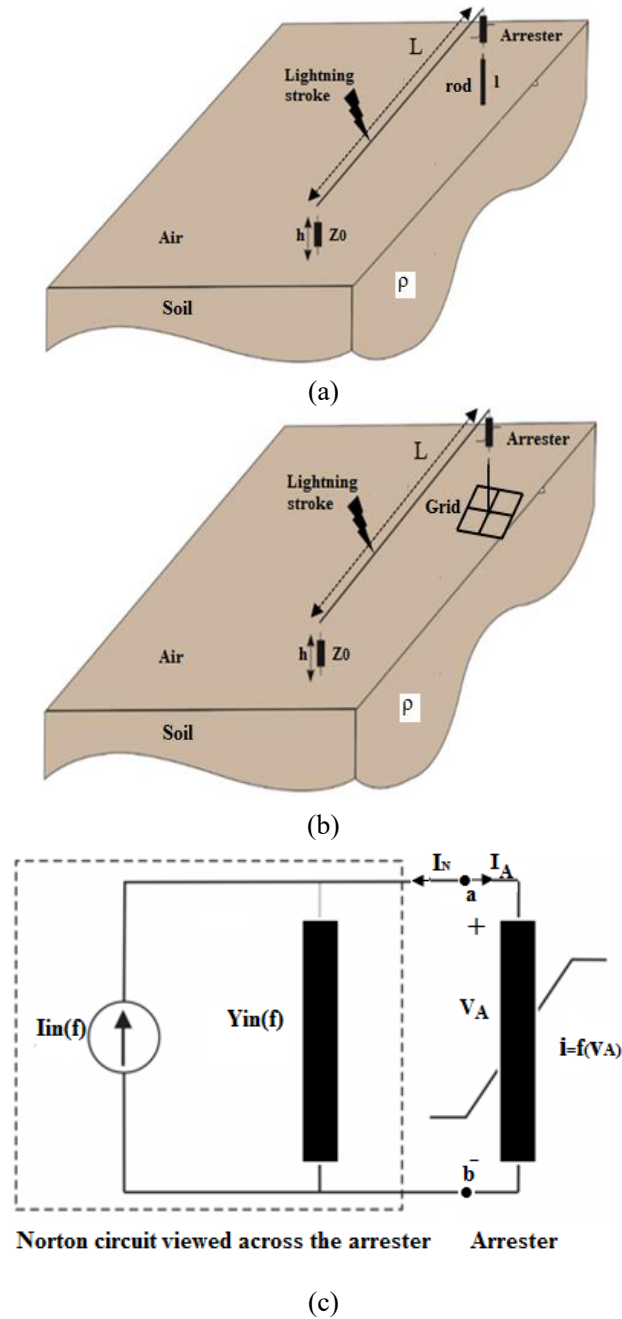
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AOM is an iterative method [10], the authors in [11] proposed an efficient hybrid model based on combining the method of fuzzy (MoF) and intelligent water drop algorithm (IWD) to overcome the mentioned drawbacks.

To the best of my knowledge, there is no formula for the overvoltage of overhead lines with arrester termination except the one in [12, 13] extracted without considering the arrester based on curve-fit methods. Hence, without losing generality, a qualitative model based on adaptive-network-based fuzzy inference systems (ANFIS) [14] for predicting the overvoltage only for direct strike is proposed. The same approach can be similarly carried out for indirect strikes. Using this model, the overvoltage across the arrester in the presence of soil of constant electrical parameters is first efficiently computed. After that, using the approximation of equivalent frequency in dispersive soils [15], and the equivalent resistivity concept in two-layer soils [16], the effects of dispersion and in-homogeneity separately and simultaneously can be easily integrated with the first-created model.

This paper is organized as follows. In section 2, exact and approximate models for the problem under consideration are proposed. Section 3 is focused on the sensitivity analyses of the parameters affecting the overvoltage. Section 4 investigates the accuracy of simulation results based on the ANFIS model. As the last final achievement of this study, the capability of the proposed model in dispersive and in-homogenous soils is investigated in section 5. Finally, conclusions are given in section 6.





**Fig. 1. A transmission line under direct strike with an arrester grounded with (a): a vertical rod, and (b): a grid as well as (c); a nonlinear microwave circuit for Figs. 1(a) and (b), [8].**

## 2- MODELING PRINCIPLES

Fig. 1 shows the schematic of the single-conductor overhead line terminated to an arrester as well as its microwave equivalent circuit. In Fig. 1(a) and (b), the overhead line with length  $L$  is located at height  $h$  from a lossy soil with resistivity  $\rho$  and relative permittivity  $\epsilon_r$ . It is also matched at the left side via a characteristic impedance  $Z_0$ , while at the right side, it is ended with an arrester. The arrester is connected to a vertical rod of length  $l$  and a  $2 \times 2$  grid as shown respectively in Figs. 1(a) and (b). The microwave equivalent circuit in Fig. 1(c) consists of two parts. The first part is a Norton equivalent circuit viewed across the arrester, while the second part is a

nonlinear load to model the arrester.

Note that the wide-band input impedance of the two grounding systems is included in Fig.1(c) below

$$I_{sc} = \frac{I_{sc}^{TL}}{1 + Z_{in}^G Y_{in}^{TL}} \quad (1)$$

$$Y_{in} = \frac{Y_{in}^{TL}}{1 + Z_{in}^G Y_{in}^{TL}} \quad (2)$$

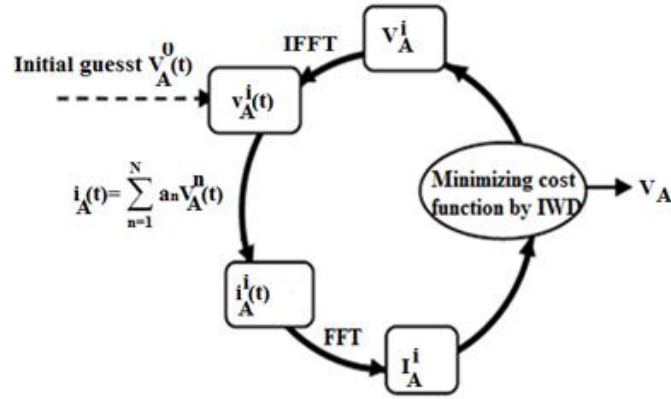


Fig. 2. Iteration process in the exact model for computing overvoltage.

In (1), and (2),  $I_x^T$ , and  $Y_n^T$  are respectively short circuit current and input admittance of the transmission line, while  $Z_{in}^G$  is the input impedance of the two grounding systems.

In this section, exact and approximate models respectively based on [11] and ANFIS for computing the overvoltage is briefly presented.

2- 1- Exact Model

In the exact model, at first, applying KCL in the frequency domain at node ‘a’ in Fig. 1 (c) yields:

$$I_N + I_A = 0 \tag{3}$$

Where  $I_N$  and  $I_A$  are respectively Norton’s circuit and arrester current vectors. Substituting  $I_N$  from Fig. 1(c) in (1), we have

$$-\bar{I}_{in} + \bar{Y}_{in} \times \bar{V}_{NL} + \bar{I}_A = 0 \tag{4}$$

Where  $\bar{Y}_{in}$  is the input admittance matrix at mixing frequencies. Also,  $\bar{I}_{in}$  is computed only at  $k$  exciting frequencies inside the lightning current content, i.e.

$$\bar{I}_{in} = [I_{in,0}, I_{in,1}, \dots, I_{in,k}, \dots, 0, 0] \tag{5}$$

whereas  $\bar{I}_A$  and  $\bar{V}_A$  are computed at  $k'$  mixing frequencies ( $k' > k$ ), i.e.,

$$(5) \bar{I}_{in} = [I_{in,0}, I_{in,1}, \dots, I_{in,k}, \dots, 0, 0] \tag{6}$$

$$\bar{V}_A = [V_{A,0}, V_{A,1}, \dots, V_{A,2k}]; \tag{7}$$

The corresponding time-domain expressions for the above

mentioned quantities are as below

$$i_A(t) = I_{A,0} + \left( \sum_{n=1}^{k'} I_{A,2p-1} \cos \omega_p t + I_{A,2p} \sin \omega_p t \right) \tag{8}$$

$$v_A(t) = v_{A,0} + \left( \sum_{p=1}^{k'} v_{A,2p-1} \cos \omega_p t + v_{A,2p} \sin \omega_p t \right) \tag{9}$$

In (4),  $\bar{I}_A$  can be expressed versus  $\bar{V}_A$  in the frequency domain as below

$$\varepsilon = -\bar{I}_{in} + \bar{Y}_{in} \times \bar{V}_{NL} + \bar{T}f(\bar{T}^{-1} \bar{V}_A) \rightarrow 0 \tag{10}$$

Where  $\bar{T}$  and  $\bar{T}^{-1}$  are transformation matrices from time domain to frequency domain and vice versa. Substituting (9) in (4), the following cost function is achieved.

$$\mu(x) = \exp \left[ - \left( \frac{x - c_i}{\sigma_i} \right)^2 \right] \tag{11}$$

Solving the above cost function based on IWD algorithm [17-19],  $\bar{V}_A$  and accordingly  $v_A(t)$  is computed. Fig. 2 shows the flow chart of the exact model.

2- 2- Approximate Model

In contrast with the exact model, an efficient approximate model based on the ANFIS algorithm could be used. ANFIS is a class of adaptive networks that are functionally equivalent to fuzzy inference systems (FIS). The ANFIS architecture consists of a fuzzy layer, product layer, normalized layer, defuzzy layer, and summation layer. A typical architecture of ANFIS is depicted in Fig. 3, in which a circle indicates a fixed node, whereas a square indicates an adaptive node. The ANFIS used in this paper consists of different layers as follows.

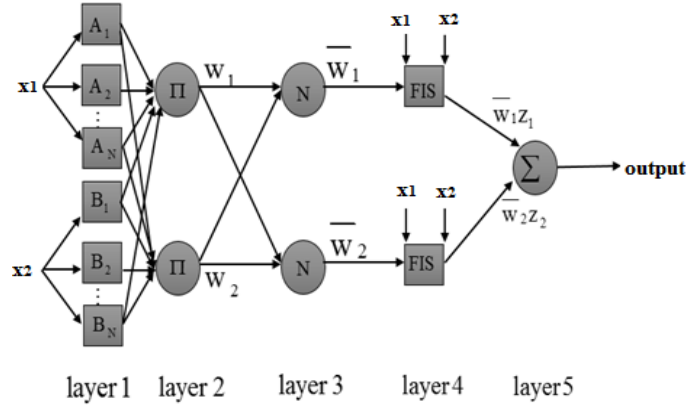


Fig. 3. Schematic of ANFIS modeling approach for nonlinear mapping with two inputs, adapted from [14].

Table 1. Parameters of the arrester in this study.

p(kA)	q	v <sub>ref</sub> (kA)
1	4	49

Layer 1: In this layer, all inputs are changed into fuzzy inputs. To this end, membership functions of the following form are used.

$$w_i = \mu_{A_i}(x_1)\mu_{B_i}(x_2), i=1,2 \tag{12}$$

where \$c\_i, \sigma\_i\$ are parameters changing the shape of membership functions and defined in such a way that each membership function has a belongingness value of one at each sampled input and is smoothly decreasing at the neighbor sampled inputs. Variable ‘x’ is a symbol for each input.

Layer 2. In this layer, the weighting for each rule is computed as below

$$w_i = \mu_{A_i}(x_1)\mu_{B_i}(x_2), i=1,2 \tag{13}$$

Layer 3. In this layer, all weightings in the previous layer are normalized, that is

$$\bar{w}_i = \frac{w_i}{w_1 + w_2}, i=1,2 \tag{14}$$

Layer 4. This layer is called TSK fuzzy inference system (FIS). This layer consists of a number of following if-then rules:

$$\text{Rule : if } x_1 \text{ is } A_i \text{ and } x_2 \text{ is } B_i \text{ then output} = p_i x_1 + q_i x_2 + k_i \tag{15}$$

where \$A\_i, i=1,2,\dots,N\$, and \$B\_i, i=1,2,\dots,N\$ are the membership functions as defined in (1). Also \$p\_i, q\_i, k\_i\$ are constants determined using least square technique in training process to decrease the predefined error.

Layer 5. In this layer, all weighted outputs of FISs are combined, so that the overvoltage is computed as below

$$\text{Output}(x_1, x_2) = \sum_{i=1}^2 \bar{w}_i z_i = \sum_{i=1}^2 \bar{w}_i (p_i x_1 + q_i x_2 + r_i) \tag{16}$$

Further information in this regard can be found in [14]

### 3- SENSITIVITY ANALYSIS

Consider the overhead line in Fig. 1 having length \$L=1\$ km, and radius 2.7 cm and terminated to an arrester at right side and matched at left side. There are a number of models for arresters for instance [20, 21]. In this study, without losing generality, it is expressed as a nonlinear resistance [21]. It has been also used in [6, 7].

$$i = p \left( \frac{v}{v_{ref}} \right)^q \tag{17}$$

Where \$i\$ and \$v\$ are the arrester voltage and current, respectively; \$p, q\$, and \$v\_{ref}\$ are constants. Table 1 tabulates the selected parameters for this arrester the same as [8].

Now, all parameters which may affect the overvoltage are investigated. They are overhead line height (\$h\$), resistivity of soil (\$\rho\$), length of overhead line (\$L\$) and grounding system length (\$l\$).

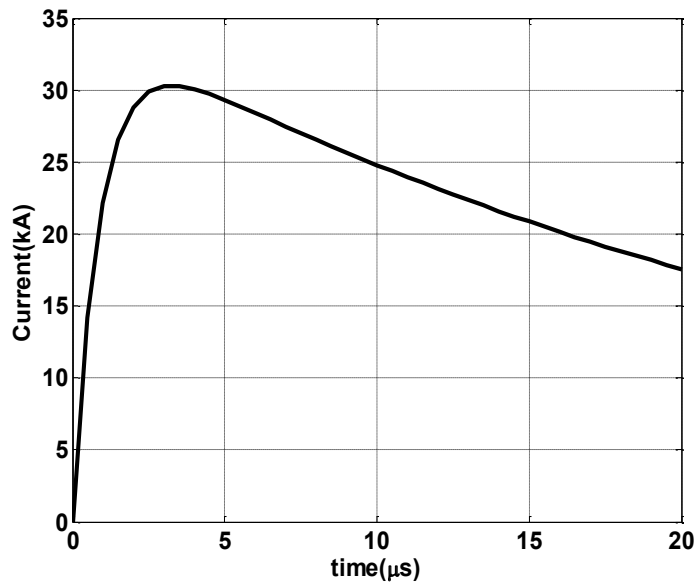


Fig. 4. Typical I waveform for the lightning current in this study and expressed as 2/20μs-30kA [8].

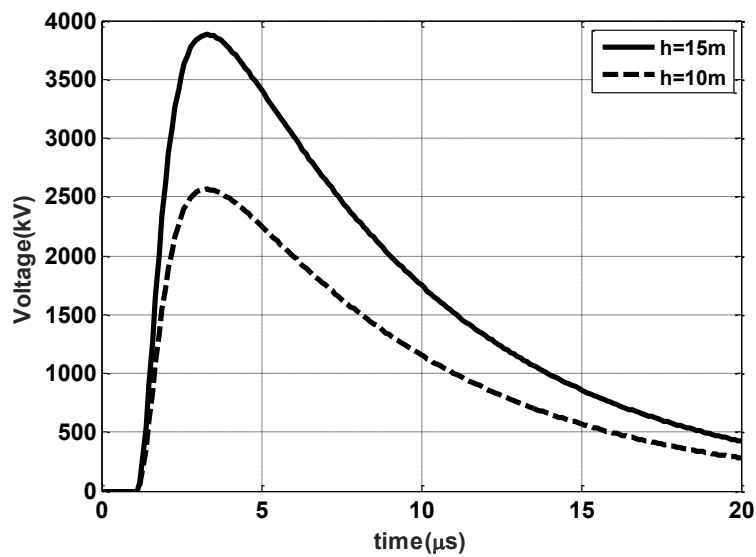


Fig. 5. Variation of transient voltage versus overhead line height (h) under assumption of  $l=3m$ ,  $\rho=100 \Omega m$ .

All simulations based on the exact model are carried out by a lightning current with double-exponential waveform, i.e., 2/20μs-30kA as shown in Fig.4. It injects to the middle of the overhead line. Prior to analysis, it is fitted with three sinusoidal waveforms, i.e.  $k=3$ , in the time interval of interest.

Figs. 5, 6, and 7 illustrate the variations of the transient

voltage versus  $\rho$ ,  $h$ ,  $l$ . As seen, the three parameters affects the overvoltage so that they can be used as variables. Also, as shown in Fig. 8, the time delay on the transient voltage is created. It is physically due to the EM waves propagation speed. Therefore it is disregarded as an input except for very long length.

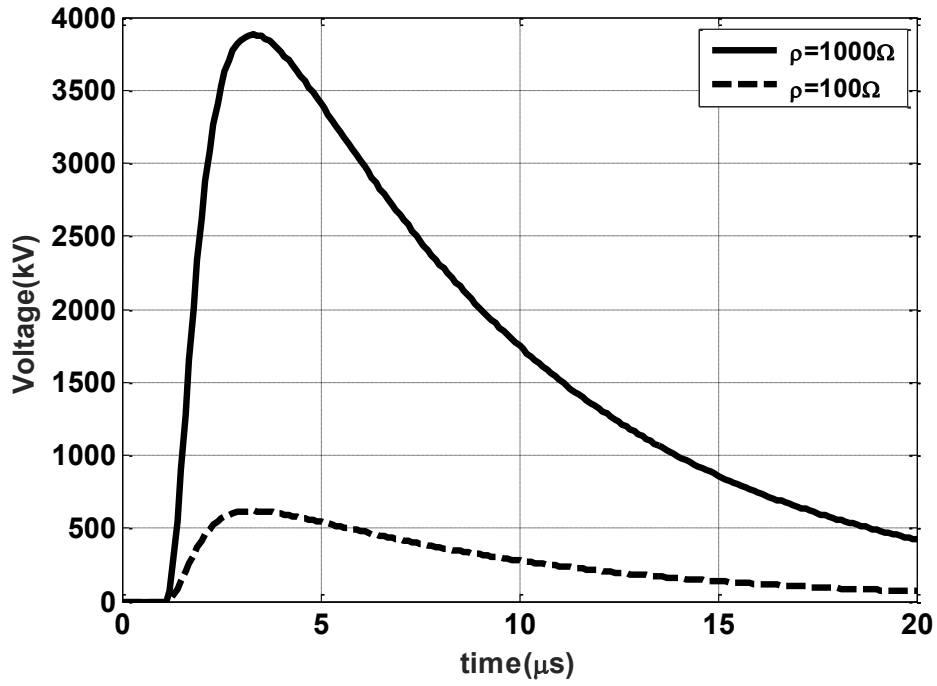


Fig. 6. Variation of transient voltage versus lossy soil resistivity ( $\rho$ ) under assumption of  $l=3m$ ,  $h=10m$ .

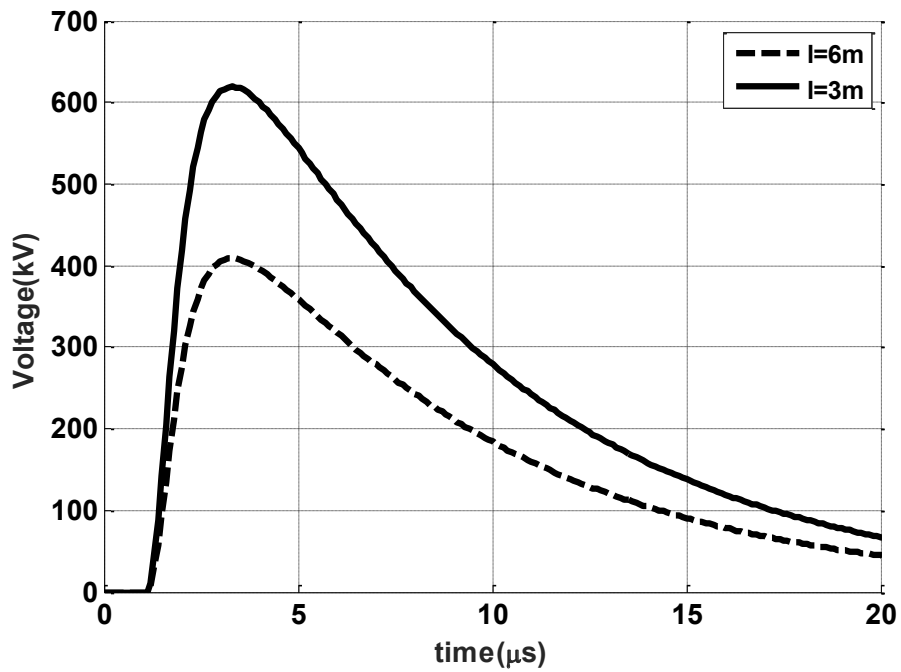


Fig. 7. Variation of transient voltage versus vertical electrode length ( $l$ ) under assumption of  $h=10m$ ,  $\rho=100\Omega m$ ,  $l=3m$ .

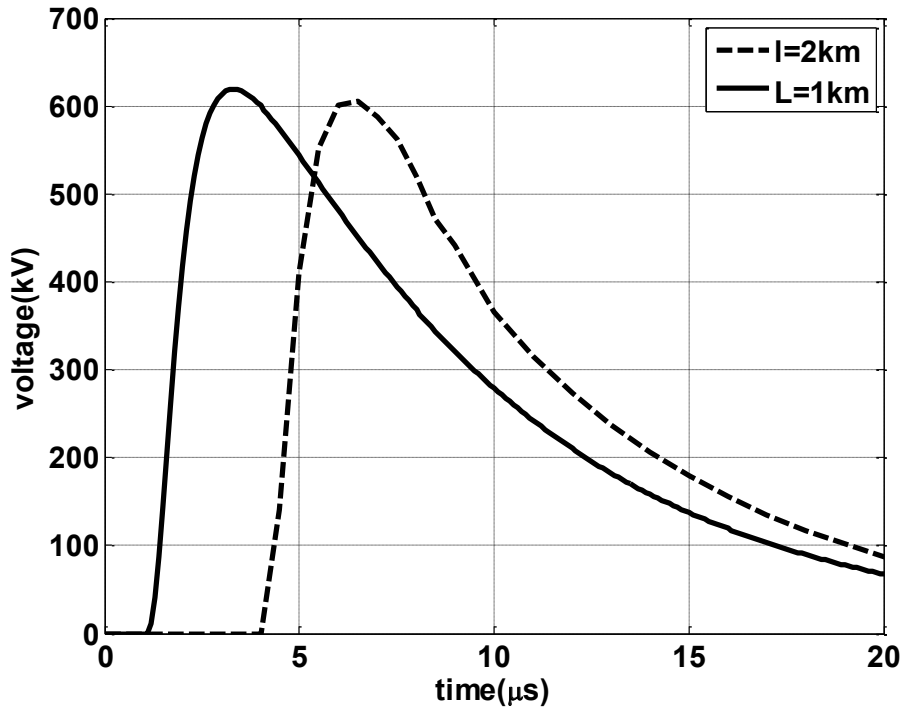


Fig. 8. Variation of transient voltage versus overhead line length (L) under assumption of  $h=10\text{m}$ ,  $\rho=100 \Omega\text{m}$ ,  $l=3\text{m}$ .

#### 4- NUMERICAL RESULTS

According to the above findings, now a closed-form expression for the overvoltage as an output versus the three inputs including  $h$ ,  $l$ , and  $\rho$  based on ANFIS technique is extracted. To this end without losing generality, five samples for  $\rho$  in the intervals of  $[100,1000]\Omega\text{m}$ , 3 samples for  $l$  in the interval of  $[3,9]\text{m}$  and 9 samples for  $h$  in the intervals of  $[0, 8]\text{m}$  are first selected. These intervals can be extended. The corresponding outputs are computed based on the exact model [11] and then used in the training process (totally  $5 \times 9 \times 3 = 135$  input-output samples are needed). The root mean square error (RMSE) for both grounding systems are shown in Fig. 9. As can be seen, after 10 epochs, the iteration processes for both grounding systems are converged. Accordingly, the adjusted membership functions are extracted and shown in Fig. 10. Now the created ANFIS algorithm can be used for predicting the overvoltage efficiently for arbitrary values of inputs. In prediction phase, assume that the vertical rod is of length  $l=3\text{m}$  and the grid is an equally-spaced  $2 \times 2$  square with meshes  $5\text{m} \times 5\text{m}$ , while  $h$  and  $\rho$  are varied.

Figs. 11 and 12 show the ANFIS-based overvoltage respectively when the resistivity is constant and height is variable, and vice versa. In both figures, the simulation results based on the exact model in [11] are also included with the aim of comparison. The comparison shows excellent agreement. Table 1 compares the run times of different models for computing the overvoltage as well. As can be seen, among different models, ANFIS has the lowest run time

which is practically of importance.

#### 5- APPLICATION TO COMPLEX SOILS

##### 5- 1- Dispersive Soils

As an application of the proposed model, it can be used in computing overvoltage when the electrical parameters of soil are frequency-dependent (dispersive soil). To this aim, at first, the frequency variations of resistivity and relative dielectric constants of soil are assumed to be computed as below [22]

$$\rho(f) = \rho_0 \left( 1 + \left( 1.2 \times 10^{-6} \times \rho_0^{0.73} \right) (f - 100)^{0.65} \right)^{-1} \quad (18)$$

$$\epsilon_r(f) = \begin{cases} 192.2 & f \leq 10\text{kHz} \\ 1.3 + 7.6 \cdot 10^3 \cdot f^{-0.4} & f \geq 10\text{kHz} \end{cases} \quad (19)$$

In (18) and (19),  $\rho_0$  and  $f$  are respectively low-frequency resistivity of soil in  $\Omega\text{m}$  and frequency in Hz.

With reference to [15], the inclusion of soil dispersion can be approximately considered at the equivalent frequency  $f_q = 1/4T_r$  where  $T_r$  is the rise time of the lightning current waveform. For the lightning current as shown in Fig. 10, it is 31.25 KHz which leads to the equivalent resistivity and relative dielectric constant respectively  $\rho_q = 400\Omega\text{m}$  and  $\epsilon_{req} = 127$ . Now substituting  $\rho_q$  instead of  $\rho$ , the overvoltage can be easily computed in dispersive soils. Figs.

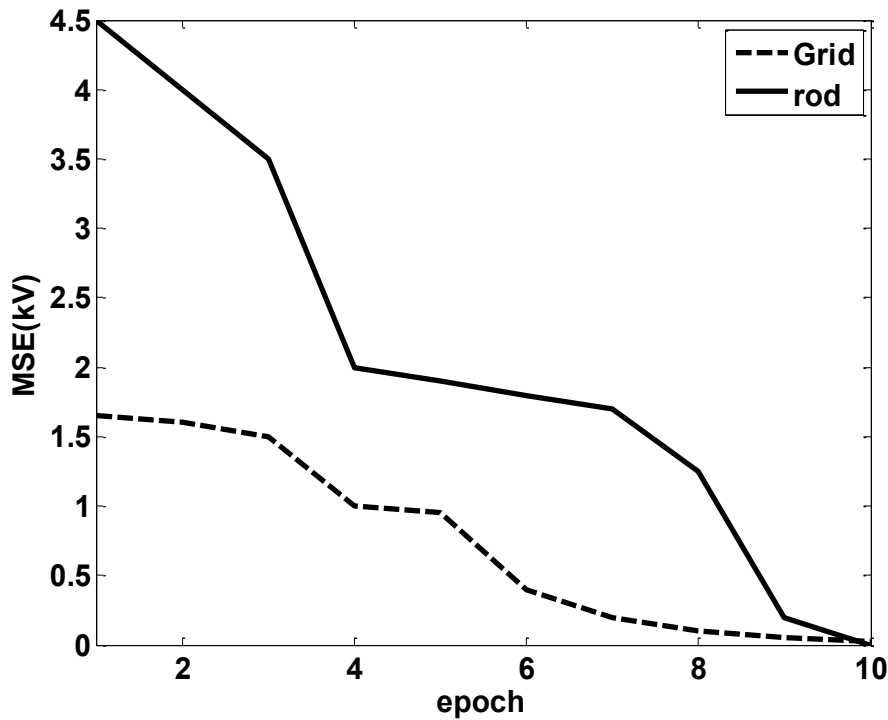


Fig. 9. Mean square errors (MSE) versus epoch in the training process for the rod and grid networks.

13 and 14 show the overvoltage across the arrester based on the ANFIS model and the ones in [23] versus the height and low-frequency resistivity. As can be seen in Fig. 13, good agreement between the ANFIS and [23] is achieved, whereas in Fig. 15, when the height is increased the results of the ANFIS and [23] are diverged since in [23] the Norton’s circuit parameters are computed based on BLT equations which are restricted to condition  $kh \ll 1$ .

Evidently, such violation will be more increased for fast-front currents since this condition is no longer satisfied.

### 5- 2- Two-Layer Soils

As another application of the closed-form expression achieved for the overvoltage, it can be used in horizontally two-layered soil. To this end, the equivalent resistivity concept [16] as expressed in (20) can be used.

$$\rho_{eq} = \rho_1 \left[ \frac{(\sqrt{\rho_2 + \sqrt{\rho_1}}) + (\sqrt{\rho_2 - \sqrt{\rho_1}})e^{-2d\sqrt{\pi f \mu_0 / \rho_1}}}{(\sqrt{\rho_1 + \sqrt{\rho_2}}) - (\sqrt{\rho_2 - \sqrt{\rho_1}})e^{-2d\sqrt{\pi f \mu_0 / \rho_1}}} \right]^2 \quad (20)$$

In (18),  $\rho_1$  and  $\rho_2$  are respectively resistivity of the upper and lower layers. Also,  $d$  is denoted for upper layer thickness. The frequency  $f$  in (20) is equal to 124 kHz for the first stroke current and 516 kHz for the subsequent stroke current [24]. As stated in [16], this approximation leads to good agreement, except that the difference of the resistivity

values of the two layers is increased and the upper layer thickness is decreased. The error will be more pronounced for subsequent stroke current (see Table I and Fig. 4 in [16]).

Integration of this approximation with the time-consuming finite difference time domain method (FDTD) has been used for transient analysis of the overhead lines over two-layer soils in the absence of arresters successfully [25].

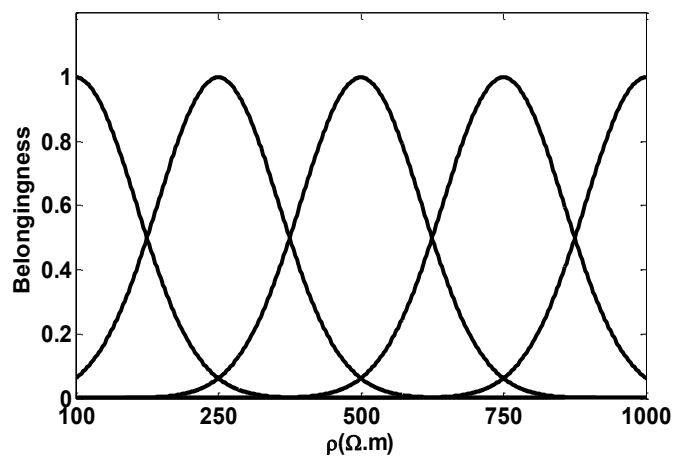
To investigate the validity of the proposed model in two-layer soils, it is assumed that the resistivity values of the upper and lower layers are  $\rho_1 = 1000 \Omega m$  and  $\rho_2 = 100 \Omega m$  respectively. Fig. 15 shows the ANFIS-based overvoltage across the arrester versus the upper layer thickness. In addition, the overvoltage in single-layer soils are included. As can be seen, except for the low-valued thickness, good agreement between the ANFIS model and [26] is achieved.

### 5- 3- Dispersive and Two-Layer Soils

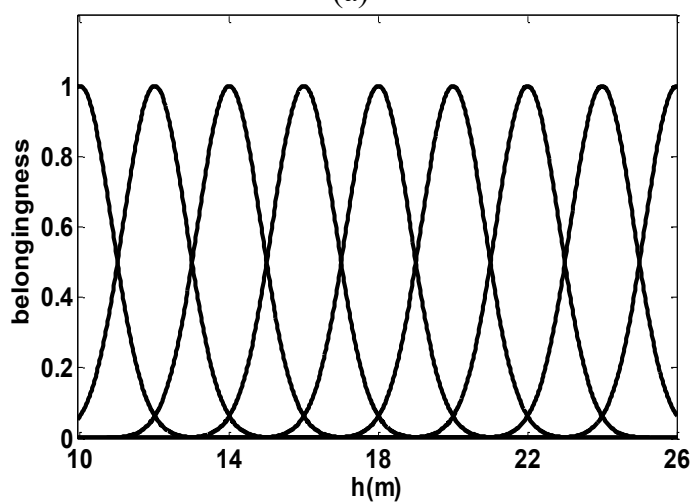
Finally, the efficient expression can be used in soils where dispersion and non-homogeneity simultaneously occur. To this aim, low-frequency equivalent resistivity, i.e.  $\rho_{0eq}$ , instead of  $\rho_0$  in (20) is replaced

$$\rho_{0eq} = \rho_{01} \left[ \frac{(\sqrt{\rho_{02} + \sqrt{\rho_{01}}}) + (\sqrt{\rho_{02} - \sqrt{\rho_{01}}})e^{-2d\sqrt{\pi f \mu_0 / \rho_{01}}}}{(\sqrt{\rho_{01} + \sqrt{\rho_{02}}}) - (\sqrt{\rho_{02} - \sqrt{\rho_{01}}})e^{-2d\sqrt{\pi f \mu_0 / \rho_{01}}}} \right]^2 \quad (21)$$





(a)



(b)

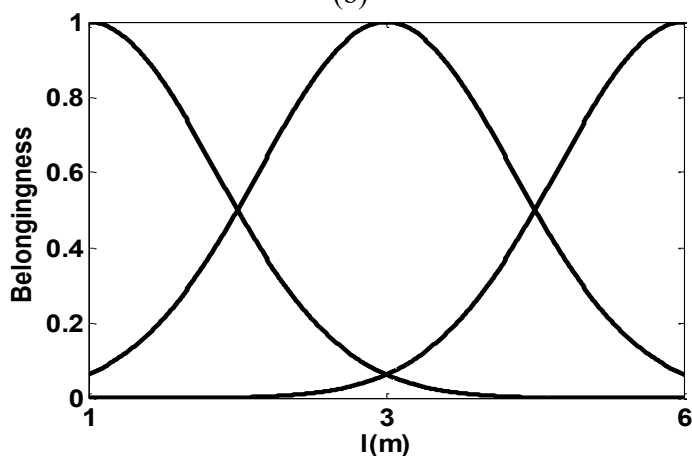


Fig. 10. Adjusted membership functions versus the three input variables, (a):  $\rho$ , (b):  $h$ , and (c):  $l$ .

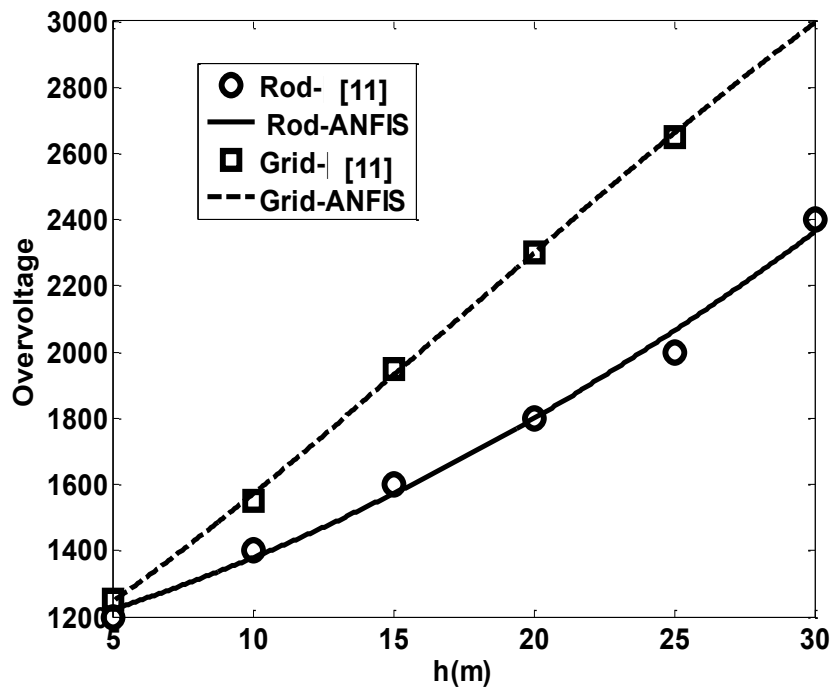


Fig. 11. Comparison of predicted overvoltages (kV) based on the ANFIS and [11] with  $\rho = 500\Omega\text{m}$ .

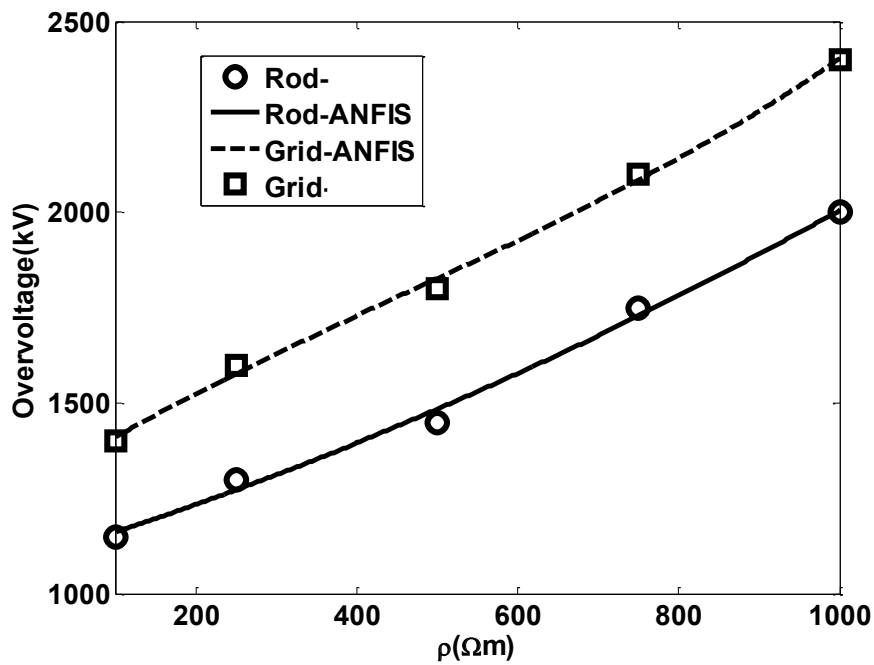


Fig. 12. Comparison of predicted overvoltages based on the ANFIS and [11] with  $h=10\text{m}$ .

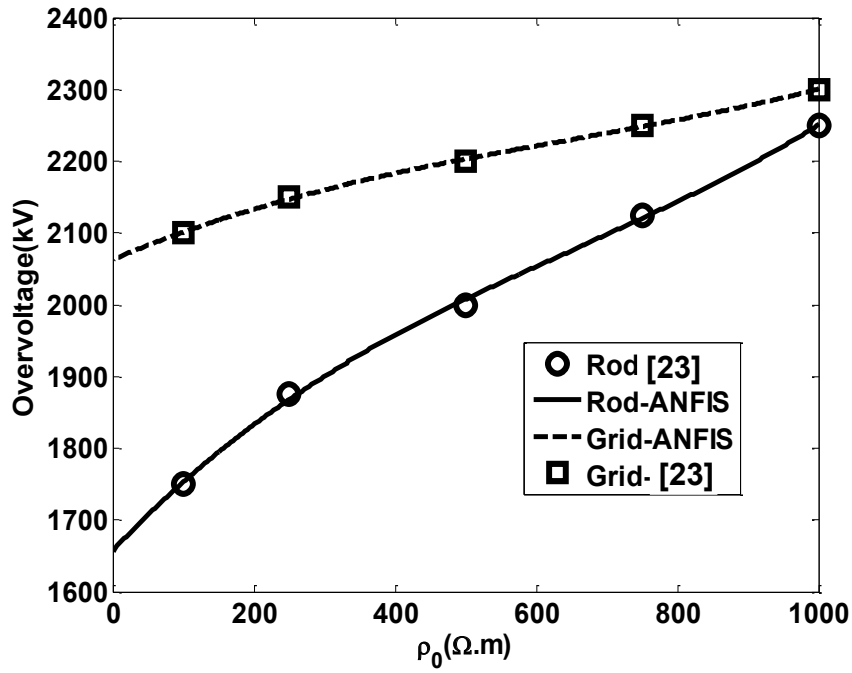


Fig. 13. Predicted overvoltages based on the ANFIS model and [23] in dispersive soils versus the low-frequency resistivity ( $\rho_0$ ) under assumption of  $h=0$ .

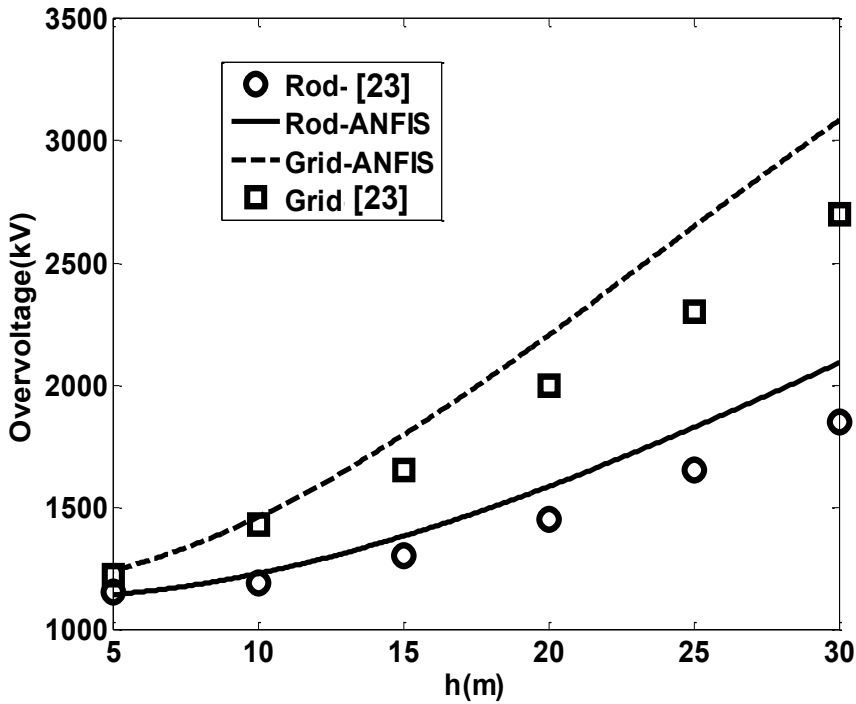
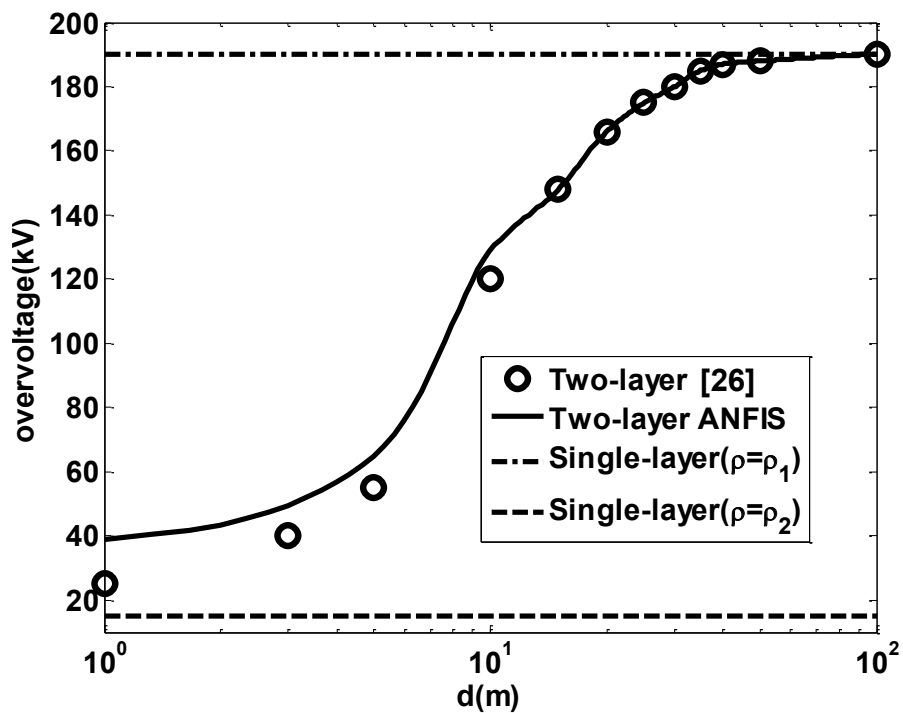


Fig. 14. Predicted overvoltages based on the ANFIS model and [23] in dispersive soils versus the height of the transmission line ( $h$ ) under the assumption of  $\rho_0 = 500\Omega$ .

**Table 2. Comparison of run times (sec) of the different methods for computing the overvoltage.**

Method	[11]	BLT-AOM [7]	This paper
Ground	Rod	9	19
	Grid	11	21



**Fig. 15. ANFIS-based overvoltages versus the upper layer thickness in two-layer soils and comparison with [26] as well as single-layer ones.**

To illustrate this situation of soil, it is assumed that the low-frequency resistivity values of upper and lower layers are respectively  $1000\Omega\text{m}$  and  $100\Omega\text{m}$ . the upper layer thickness is assumed to be 10m. Fig. 16 shows the overvoltage for such soil. With the aim of comparison, the single-affected soils including dispersive single-layer soils with low-frequency resistivity equal to the low-frequency resistivity of the upper and lower layers ( $\rho_0=1000, 100\Omega\text{m}$ ) and non-dispersive two-layer soil ( $\rho_1=1000, \rho_2=100\Omega\text{m}$ ) are included in this figure as

well. From this figure, two notes are inferred. The first is that the overvoltage in dispersive and two-layer soil is a middle value between the individual ones in dispersive and single-layer soils having the low-frequency resistivity of upper and lower layers. The second is that the overvoltage in dispersive and two-layer soil is greater than that of non-dispersive and two-layer soil. The mentioned findings play an important role in selecting lightning arresters which should be considered by power engineers.

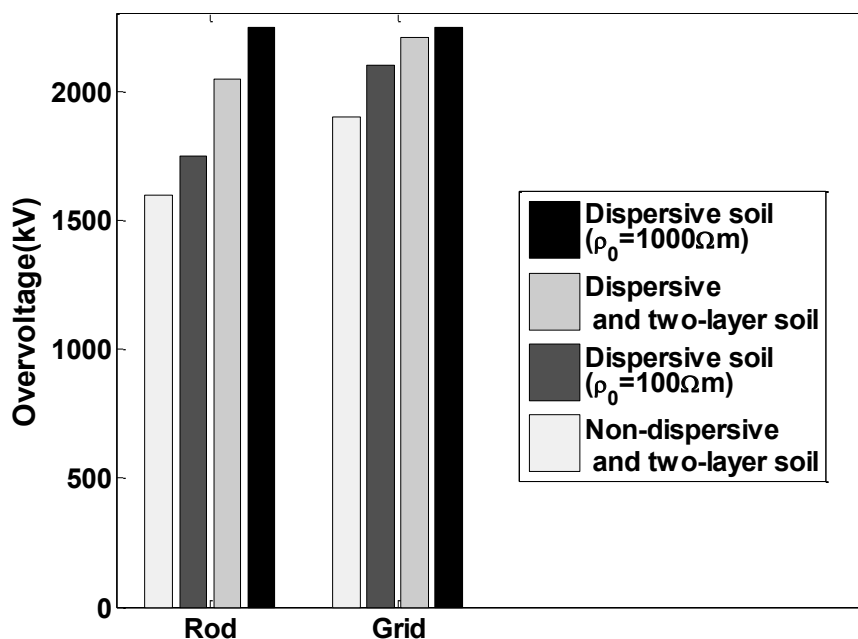


Fig. 16. ANFIS-based overvoltages in dispersive and two-layer soils and comparison single-affected soils.

## 6- conclusion

In this paper, the application of the ANFIS algorithm was proposed for comprehensive and broad-band prediction of overvoltage of single-phase overhead lines terminated with arresters. The electrical parameters of the lossy soil can be constant, frequency-dependent, and in-homogenous. Due to its efficiency, it plays an important role when the weather conditions are changed since repetitive and time-consuming computations are removed.

Extending the proposed model to single and three-phase overhead lines considering the nonlinear phenomenon of ionization and front time is in progress. In such cases, ANFIS technique may be violated results since the number of inputs increased. To remove this drawback, spatial membership functions [27, 28] can be used.

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