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Dynamic Performance Analysis of High-Frequency Signal Injection Based Sensorless Methods for Application in Interior Permanent Magnet Synchronous Motors

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ABSTRACT: This paper focuses on three commonly used sensorless methods based on high-frequency signal injection; namely, the rotating sinusoidal injection in the stationary reference frame, the pulsating sinusoidal injection in the estimated synchronous reference frame, and the pulsating square wave injection in the estimated synchronous reference frame. These methods have found applications in interior permanent magnet synchronous motor (IPMSM) sensorless drives. Some efforts have been performed to compare such high frequency signal injection-based methods from the viewpoint of some parameters such as injection frequency, voltage magnitude, etc. However, the evaluation of their dynamic seems to await further investigation and evaluation. Hence, some of the motor parameters such as pole number, machine saliency ratio, that affect the performance of the saliency-based sensorless methods are evaluated in this paper. Moreover, some such other parameters in driver circuit such as current measurement noise, the effect of time delay on demodulation, and load disturbance effect are also explored. The maximum torque per ampere (MTPA) strategy is employed to improve motor driven torque and overcome the load torque by using reluctance torque component. Finally, simulation and experimental results are used to investigate the effects of the above parameters on the performance of high-frequency signal injection based sensorless methods.

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1- Introduction

Permanent magnet synchronous motors (PMSMs) have received much attention due to their superior advantages of high torque density per volume, performance, and reliability. Taking advantage of all the PMSM capabilities requires proper knowledge of rotor position that may be obtained from position sensors they, however, not only increase the volume, complicity, and weight of the motor-drive system but also decrease its reliability. These drawbacks motivated the development of sensorless algorithms for motor application. These algorithms may be divided into two types of standstilllow speed region methods based on the machine saliency and middle-high speed ones based on BEMF[1]. Unfortunately, BEMF based methods become useless in standstill-low speed region due to lack of BEMF in these speed values [2-8]. Instead, continuous carrier-voltage injection-based sensorless methods [9-31] are then employed due to the effectiveness at a standstill and low-speed range. For the zero- and lowspeed position estimation, the spatial information in machine saliencies is tracked for the sensorless drive. These saliencies can be estimated through the measurement of current signals with HF voltage signal persistent excitation. It is important to note that all the signal injection techniques require a certain amount of dc-bus voltage to excite the saliency signal for the position estimation. This issue limits the saliencybased drive performance as speed increases [9]. By contrast, the position estimation based on the spatial information of back electromotive force (EMF) voltage demonstrates a comparable performance without the voltage injection when the speed is beyond 5-10% rated speed [10, 11]. Thus, it is desired to implement two-position estimation methods at different speed areas for a full region sensorless drive. A transition algorithm combing two-position signals has developed for the smooth dynamic operation from zero to full speed [11-14].

The Saliency-based or High-frequency (HF) signal injectionbased sensorless methods are basically classified according to the injection signal waveform into the sinusoidal wave injection and square wave injection methods [15, 16]. The former is further subdivided into three types of rotating signal injection in the stationary reference frame, pulsating signal injection in the estimated synchronous reference frame, and anti-clockwise pulsating injection in the estimated synchronous reference frame that rotates reversely at twice rotor electrical speed [17]. These methods may also be utilized based on negative sequence current sensing and zerosequence voltage sensing. However, the negative sequence current-based method in most cases is preferred to the zerosequence voltage one due to the inaccessibility of the neutral point in machine windings [1, 15]. The square wave injection methods may also be divided into three types of rotating injection in the stationary reference frame, pulsating injection in the estimated synchronous reference frame, and pulsating injection in the anti-clockwise synchronous reference frame that rotates at twice rotor electrical speed [1, 4, 18, 19].

While some researchers regard the square wave injection methods to be superior to sinusoidal ones due to the enhanced bandwidth of the sensorless driver as a result of the higher injected frequency, it is yet this higher injected frequency that requires more injected voltage amplitude, which then increases the high-frequency injection losses of the motor [20]. In [17], the three commonly used high-frequency

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sinusoidal injection methods are compared based on such considerations as signal delay, ease of implementation, and accuracy. Focusing on the square wave signal injection methods, [19] finds the pulsating square wave injection preferable for IPMSM sensorless drives based on current sensing.

Based on the above observations, a comprehensive understanding of the dynamic performance of HF injection methods seems to require further investigation. The present study was, therefore, designed and implemented to carry out a comprehensive comparison of HF injection-based sensorless methods considering such different parameters as machine pole number, saturation effect on machine saliency, and thereby the performance of the sensorless method. Moreover, the effects of such parameters as current measurement noise, time delay effect due to signal demodulation, and load disturbance effect are investigated. Given the greater advantages of pulsating sinusoidal injection, rotating sinusoidal injection, and pulsating square wave injection methods over the other HF signal injection based sensorless methods [4, 15, 17], the present study focuses on these three methods. To achieve these objectives, experiments and simulations were conducted and the results obtained were subjected to analysis in MATLAB.

2- Hf Signal Injection Principle

The dynamic model of an IPMSM can be described as,

$$\begin{bmatrix} v_q \\ v_d \end{bmatrix} = \begin{bmatrix} r_s + L_{sq}p & -\omega_e L_{sd} \\ \omega_e L_{sq} & r_s + L_{sd}p \end{bmatrix} \begin{bmatrix} i_q \\ i_d \end{bmatrix} + \begin{bmatrix} 0 \\ \omega_e \psi_m \end{bmatrix}.$$
(1)

For the high-frequency injection-based sensorless methods at stand-still and low-speed regions, BEMF can be neglected and cross-coupling term is also small, thus it can also be ignored. With these assumptions, equation (1) can be simplified and presented as an inductive load circuit [7]e-[21]

$$\begin{bmatrix} v_q^h \\ v_d^h \end{bmatrix} = \begin{bmatrix} X_q^h & 0 \\ 0 & X_d^h \end{bmatrix} \begin{bmatrix} i_q^h \\ i_d^h \end{bmatrix},$$
 (2)

where index h denotes the "High-Frequency."

The flux linkage equation in the stationary reference frame for the interior permanent magnet synchronous motors is captured by (3) below [22]

$$\begin{bmatrix} \lambda_q^s \\ \lambda_d^s \end{bmatrix} = \begin{bmatrix} L_{sum} + L_{diff} \cos 2\theta_e & -L_{diff} \sin 2\theta_e \\ -L_{diff} \sin 2\theta_e & L_{sum} - L_{diff} \cos 2\theta_e \end{bmatrix} \begin{bmatrix} i_q^s \\ i_d^s \end{bmatrix} (3)$$

where $L_{sum} = \frac{L_d + L_q}{2}$. $L_{diff} = \frac{L_d - L_q}{L_q^2}$ are average and differential inductance, L_d and L_q^2 are d and q-axes inductance,



Fig. 1 Coordinate reference frame for HF rotating sinusoidal injection in the stationary reference frame

 i_d^s . i_q^s and λ_d^s . λ_q^s are d and q-axes currents and fluxes in the stationary reference frame, respectively. In the estimated synchronous reference frame by using park transformation, d and q-axis currents can be driven from (3) as[23]:

$$\begin{bmatrix} i_{qi}^{e} \\ i_{di}^{e} \end{bmatrix} = \frac{L_{sum}}{det(L)} \int_{v_{di}}^{v_{qi}^{e}} \end{bmatrix} + \frac{L_{dif}}{det(L)} \begin{bmatrix} -\cos(2\theta_{r} - 2\theta_{e}) & \sin(2\theta_{r} - 2\theta_{e}) \\ \sin(2\theta_{r} - 2\theta_{e}) & \cos(2\theta_{r} - 2\theta_{e}) \end{bmatrix} \int_{v_{di}}^{v_{qi}^{e}} \end{bmatrix}$$
(4)

where, v_{qi}^{e} , v_{di}^{e} , i_{qi}^{e} , and i_{di}^{e} are injected carrier voltages and resultant currents in the estimated synchronous d-q axes and $\int (.)$ represents the integration operator.

It should be noted that equation (4) is valid for the highfrequency injection method in the standstill and low-speed regions that may be ignored in the BEMF term in motor voltage equations. Additionally, derivation of (4) from (3) is based on the assumption that stator resistance is negligible. The equation (4) is applicable to both types of interior and surface-mounted permanent magnet synchronous motors (SPMSM) while it may also be used for the square and sinusoidal shapes of injection-based sensorless methods.

2-1-HF rotating sinusoidal injection in the stationary reference frame

Fig. 1 shows the coordinate reference frame for the HF rotating sine injection method. Clearly, a High-frequency sinusoidal voltage is applied to the α - β axes of the stationary reference frame as expressed by equation (5) below.

where, w_i and v_i represent frequency and voltage amplitude of the injected voltage, respectively. The resultant carrier current which contains information on rotor position may be obtained using (3) as in (6) below [24]:



Fig. 2 Block diagram of HF rotating sinusoidal injection method



Fig. 3. Coordinate reference frame for HF Pulsating sinusoidal injection in the estimated synchronous reference frame

$$\begin{cases} i \alpha_{i} = Re\left(LPF\left(i \alpha \beta_{i} e^{j\left(w_{i}t - \frac{\pi}{2}\right)}\right) = v_{i} \frac{Lq - Ld}{2w_{i}Ld Lq} \cos 2\theta_{e}, \\ i \beta_{i} = Im\left(LPF\left(i \alpha \beta_{i} e^{j\left(w_{i}t - \frac{\pi}{2}\right)}\right) = v_{i} \frac{Lq - Ld}{2w_{i}Ld Lq} \sin 2\theta_{e}, \end{cases}$$
(6)

where, Re(.) and Im(.) denote the real and imaginary parts of the carrier resultant current, respectively. Using such position observers as PID controller or phase loop lock (PLL), the estimated rotor position may be extracted as shown in Fig. 2.

2- 2- HF pulsating sine injection in the estimated synchronous reference frame

Fig. 3 displays the coordinate reference frame for an HF pulsating sinusoidal injection in the estimated synchronous reference frame in which the injected voltage is applied to the estimated d-axis or q-axis expressed by (7) below:

$$\begin{bmatrix} v_{di} \\ v_{qi} \end{bmatrix} = v_i \begin{bmatrix} \cos w_i t \\ 0 \end{bmatrix} \text{ or } v_i \begin{bmatrix} 0 \\ \cos w_i t \end{bmatrix}.$$
(7)

Generally speaking, it is more popular from a torque ripple minimization viewpoint to inject the high-frequency voltage to the estimated d-axis, and the resultant current on the q-axis can be considered in estimating rotor position. The position error function that contains information on rotor position is derived by substituting (7) for (4) and performing some simplification operations to yield equation (8) below [17]

$$i_{qi}^{e} = v_i \frac{z_q - z_d}{2z_q z_d} \sin 2\Delta\theta \tag{8}$$

Similar to what was observed with the rotating sine injection, rotor position and its velocity can then be tracked using a simple PID controller.



Fig. 4. The coordinate reference frame for the pulsating square wave injection in the estimated synchronous frame

2- 3- HF pulsating square wave injection in the estimated synchronous reference frame

For the pulsating square wave injection in the estimated synchronous reference frame, the voltage injected in the estimated d-axis can be written as in (9) and shown in Fig. 4.

$$\begin{bmatrix} v_q^i \\ v_d^i \end{bmatrix} = v_i \begin{bmatrix} 0 \\ \pm 1 \end{bmatrix}.$$
(9)

By substituting (9) for (4), equation (10) is obtained as the basic equation for the square wave voltage injection method:

$$\begin{bmatrix} i_{q}^{i} \\ i_{d}^{i} \end{bmatrix} = \frac{v_{i} L_{sum}}{det (L)} \begin{bmatrix} 0 \\ \pm t \end{bmatrix} + \frac{v_{i} L_{dif}}{det (L)} \begin{bmatrix} -\cos \left(2\theta_{r} - 2\hat{\theta}_{re}\right) & \sin \left(2\theta_{r} - 2\hat{\theta}_{re}\right) \\ \sin \left(2\theta_{r} - 2\hat{\theta}_{re}\right) & \cos \left(2\theta_{r} - 2\hat{\theta}_{re}\right) \end{bmatrix} \begin{bmatrix} 0 \\ \pm t \end{bmatrix}.$$
(10)

Based on the square wave shape with some mathematical calculations, the high-frequency q-axis current may be written as in (11) below [23]:

$$\begin{cases} i_q^i = \frac{\mathbf{v}_i \ L_{dif}}{\det(L)} \frac{1}{Ti \ / 2} \sin \Delta \theta t & 0 < t < \frac{T_i}{2}, \\ i_q^i = \frac{\mathbf{v}_i \ L_{dif}}{\det(L)} \frac{1}{T_i \ / 2} \sin \Delta \theta (T_i - t) & \frac{T_i}{2} < t < T_i, \end{cases}$$
(11)

where T_i represents the current sampling period. Using differential processing, equation (11) may be rewritten as:

$$\Delta i_q^i = i_q^i \left(t = \frac{T_i}{2} \right) - i_q^i \left(t = 0 \right) \approx$$

$$\frac{v_i L_{dif}}{det \left(L \right)} \frac{1}{Ti / 2} \sin \Delta \theta \cdot \frac{T_i}{2}.$$
(12)

	Speed	Current	Observer	unit
K _p	10	2	40	-
K _i	2	0.2	10	-
K _c	0.2	0.02	0.25	-
V _i		60		V
F _i		1000		Hz

Table 1. Motor controller parameters

3- Performance Analysis: Simulation And Experimental Results

In this section, evaluation of the most popular HF injection methods, i.e. rotating sinusoidal injection in the stationary reference frame, pulsating sinusoidal injection in the estimated synchronous reference frame and pulsating square wave are done. Fig. 5 depicts an overall control block diagram of the HF injection-based sensorless methods used for IPM synchronous motors. It is clear that three types of the HF injection method can be chosen depending on which coordinate reference frame or signal waveform is to be used. Rotor position and its



Fig. 5. Overall control block diagram of the HF injection-based sensorless method



velocity can be estimated using equations (6), (8), and (12) in the position estimation block shown in Fig. 5. According to Table I, all the control parameters, including speed control loop and current control loop PID coefficients as well as the amplitude and frequency of the injected voltage are kept constant in all three HF injection methods in order to make reliable comparisons possible. The D-axis current reference, id*, is calculated based on the maximum torque per ampere strategy (MTPA) as in (13) below [23]:

$$i_{d}^{*} = \frac{-\varphi_{f}}{2(L_{d} - L_{q})} - \sqrt{\frac{\varphi_{f}^{2}}{4(L_{d} - L_{q})^{2}} + i_{q}^{*2}}$$
(13)

where, φ_{f} is the magnet flux linkage.

3-1-Motor parameters effect: Pole number effect and machine saliency ratio

Fig. 6 shows the effects of increasing motor pole number on its speed response for the rotating sinusoidal injection, pulsating sinusoidal injection, and pulsating square wave injection, respectively. It is seen that rotor position error increases when the machine pole number increases from 2 to 10, resulting in an oscillatory speed response.

It is seen that the HF rotating sine wave injection is more



Fig. 7. Effects of motor saturation on the performance of the sensorless method



Fig. 8. The effect of current measurement noise on the step response of sensorless methods

stable than the other two methods because the actual measurement currents (i.e., i_a and i_b) are directly used for rotor position estimation in this method. This is while, in the other two methods, the q-axis current (i.e., i_q) is used for rotor position estimation which itself is obtained based on the estimated rotor position. Fig. 7 illustrates the effect of machine saturation on the performance of sensorless algorithms. Clearly, the saliency ratio approaches unity at machine saturation to nullify any differences between the values for d-axis and q-axis inductances. This is tantamount to the loss of the basic principle of the HF injection-based sensorless methods – that of machine saliency. However, as shown in Fig. 6b, the HF rotating sine wave injection is more stable than the other two under saturation conditions.

3- 2- Drive parameters: Time delay, Measurement noise, and load disturbance effect

Fig. 8 displays the effects of current measurement noise on the performance of HF injection-based sensorless methods. Based on equation (12), the rotating sinusoidal injection method is expected to be less sensitive to current measurement noise but the square wave injection one to be more sensitive due to the differential operation employed.

Fig. 9 depicts the performances of sensorless methods as a result of the time delay due to the signal demodulation process.



(b) Rotating sine wave injection

Fig. 9. Time delay increasing from 0 to 4 ms when the injected frequency is 1000 Hz.



Fig. 10. D-q axes currents due to the Load disturbance

This process is necessary for obtaining information on rotor position in the HF injection-based sensorless method, but it causes time delays in signal processing with a consequent adverse effect on the performance of the sensorless system.

To evaluate the effect of time delay, a delay of 0.8 milliseconds is added to the demodulation signal every PWM time interval up to a maximum of 4 milliseconds and the injection frequency is assumed to be 1000 Hz.

Based on the simulation results, the rotating sinusoidal injection method is more resistant than the other two methods to time-delay effects caused by signal demodulation process.

3-3-Load disturbance effect

The effectiveness of the three famous HF injection methods under load disturbance conditions was assessed by applying a sudden load to the motor. Figs. (10a-c) present the speed response and d-q axis currents based on the MTPA algorithm when a load disturbance is applied to the motor. Fig. 11 shows the dynamic performance of the saliency-based sensorless driver for three methods when a load torque is applied. Clearly, the rotating sinusoidal injection exhibits a slower dynamic response to load disturbance than the other two methods.



Fig. 11. Applying load torque and speed command



Fig. 12. Practical test bench

Table 2. Motor specification

Parameters	Value	Unit
Pole number	4	-
Nominal current	1.5	А
d- axis inductance	70	mH
q- axis inductance	110	mH
phase resistance	3.2	Ω
Nominal speed	1000	Rpm
Rotor Inertia	0.01	Kg.m ²
Stator Diameter	96	Mm
Stator Length	85	mm

To evaluate the effectiveness of the HF rotating sinusoidal injection, a laboratory hardware test bench was constructed using the TMS320F2812 DSP board and the intelligent power module (IPM) as a Dc-Ac inverter shown in Fig. 12. The PWM frequency and the sampling frequency were both set to 10 kHz and a 310 V DC power supply was used for the inverter. The motor parameters are listed in Table 2.

The practical results, including the actual and the estimated rotor positions, speed reference, and its estimated value are shown in Figs. (13a-b) for the HF sinusoidal rotating injection when the speed direction is reversed. Fig. 13c presents the d-axis and q-axis currents of the motor compared to their reference values. As can be seen, the d-axis reference current as calculated by the MTPA algorithm is approximately zero in the no-load conditions, indicating a reluctance torque component equal to zero. When the load is applied to the motor, however, the MTPA algorithm produces a negative d-axis reference current that leads to a positive reluctance torque. This is then added to the electromagnetic torque, which increases the overall torque output and, thereby, overcomes the load torque.



(a) Estimated and actual values of rotor position and its speed.



(b) Estimated and actual values of rotor position and its speed when rotating direction is reversed.



algorithm when a sudden load is applied to the motor.

Fig. 13 Experimental results for HF rotating sinusoidal injection used in IPMSM sensorless drive

Table 3 compares the results obtained in this study for the HF injection methods commonly used in IPMSM sensorless drives. It may be noted that this comparison is carried out among those HF injection methods that use the carrier current as a function of rotor position. Based on both simulation and practical results and according to the comparisons in Table I, the HF pulsating sinusoidal injection method based on current sensing techniques is observed to be more easily implemented than the rotating sinusoidal injection. However, the rotating sine injection seems to be less sensitive to such parameters as time delay due to demodulation, saturation effect due to load conditions, and motor pole number. Although sinusoidal HF injection methods are simple and easy to implement, their application is limited to lower injection frequencies due to

Injection method	Rotating Sine injection	Pulsating Sine injection	Pulsating square injection		
Implementation	Easy/Medium	Easy	Medium		
Signal delays	Less sensitive	Less sensitive	Sensitive		
Noise effect	Small	Small/Medium	Medium/High		
Pole number effect	Small	Small	Medium		
Saliency effect	Small	Medium	Medium		
Feasible injected frequency	Small	Small	High		

Table 3. Comparison of HF injection-based sensorless methods

the PWM frequency limitation. Instead, the HF square-wave injection method can be used at higher injection frequencies, which provides such additional advantages as enhanced system bandwidth. This study, however, assumed identical frequencies for both sinusoidal and square wave injection signals in order to concentrate on the performance of HF injection methods by assuming identical values for all the control parameters and filter coefficients.

4- Conclusion

In this paper, three of the more commonly used HF injectionbased sensorless methods (namely, the rotating sinusoidal injection in the stationary reference frames as well as the pulsating sinusoidal injection and the pulsating square wave injection methods in the estimated synchronous reference frame) were simulated and evaluated with respect to the parameters listed in Table II. The results obtained may be summarized as follows:

- In applications in which the motor has a higher pole number, the rotating sine injection seems to be more stable than the other two methods due to the smaller error position. It also seems to be less sensitive to either the current measurement noise or the signal delay effect due to signal demodulation.
- In applications with fast load dynamic changes, the rotating injection method seems to exhibit a slower dynamic response than the other methods; hence, either the pulsating square or the sine wave injection may be preferred. The rotating sine injection, however, exhibits a better performance under heavy load conditions that might be accompanied by saturation conditions.
- Despite their ease of implementation, rotating sine injection methods are limited in their application to lower injection frequencies. Meanwhile, the frequency of the injected signal can be easily increased in square wave injection methods by up to half the PWM frequency, which results in an enhanced control bandwidth.

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