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Investigating Direct Torque Control of Six-Phase Induction Machines Under Open Phase Fault Conditions

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ABSTRACT: This paper presents analysis and evaluation of classical direct torque control (DTC), for controlling a symmetrical six phase induction motor (SPIM) under open phase fault conditions. The machine has two three-phase windings spatially shifted by 60 electrical degrees. The strategy of the proposed method consists of choosing the switching modes according to the configuration of living phases in such a way that it generates vectors that have higher amplitude in α - β plane while their projections on z axis give zero or near zero amplitude vectors. The goal is reducing parasitic currents and torque ripples of SPIM under faulty mode. Based on the theoretical analysis, it will be shown that in the open phase fault conditions, the only non-pulsating operation is obtained by opening the fault three-phase winding. Experimental test results are provided o support theoretical analysis in open phase fault conditions for SPIM.

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1- Introduction

Electrical ac machines have found wide applications in the high power industries. In these cases, we need a high power and high switching frequency semiconductors. In the case that the necessary devices are unavailable, the power is divided among more than three inverter legs to reduce semiconductor ratings. In the multi-phase drive systems, the current per phase in the machine and the inverter is reduced. The most common multi-phase machine drive structure is the six- phase induction machine (SPIM), which has two sets of three-phase windings spatially shifted by 60 electrical degrees (Figure 1). In this structure, the loss of one machine's phase does not prevent the machine from working, thus, improving the system reliability [1].

One of the most important faults in the electrical drives is the suppression of one or more stator phases of the motor. This fault disturbs the rotating MMF and produces a high pulsating torque [2]. As the dynamic behaviour of the electrical machines is very important in the modern drive systems, it is essential to develop a control method to improve the behaviour of the machine under open phase fault conditions. This paper introduces SPIM control under open phase fault conditions by DTC. Over almost a decade, several schemes have been proposed for the operation of multi-phase induction machines under open phase fault conditions based on FOC [3-5]. In FOC structure and post fault situation, the task of controllers is complicated that need to become a resonant [4] or include feedforward terms [6]. Current references also should be modified in order to obtain a sinusoidal rotating MMF [7-8] and minimum torque pulsations [3-9].

To simplify the control scheme and to improve the dynamic

performance by eliminating the current control loops, one may propose a DTC solution as an alternative to FOC schemes. Unlike FOC, DTC does not tend to duplicate the electromechanical behaviour of a dc motor drive but is aimed at a complete exploitation of the flux and torque-producing capabilities of an induction machine fed by an inverter. In this regard, DTC can be viewed as a novel technique for controlling the induction machine drive under fault conditions.

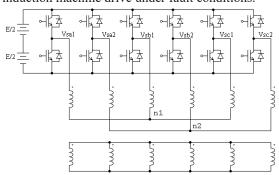


Fig. 1. SPIM with its inverter.

In this paper, the control of SPIM by DTC in the open phase fault conditions is investigated. This paper is organized into six sections. The model of the machine is presented in the next section. The control method by DTC will be discussed in section 3. Section 4 introduces the control of SPIM by DTC in normal and open phase fault conditions by experimental results. Finally, some conclusions and perspectives will be given in Section 5.

2- MODEL OF SPIM

2- 1- Model in the normal operation

The model of SPIM under normal operating conditions has

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been demonstrated in [2]. In the normal mode, the SPIM is a double-six-dimensional system (six stator and six rotor variables). It is shown in [10] that the SPIM model can be decomposed into three two dimensional orthogonal subspaces, namely (α, β) , (z1, z2), and (z3, z4), as follows:

Machine model in α - β subspace

The stator and rotor voltage equations are:

$$\begin{bmatrix} v_{s\alpha} \\ v_{s\beta} \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} r_s + L_s p & 0 & Mp & 0 \\ 0 & r_s + L_s p & 0 & Mp \\ Mp & \omega_r M & r_r + L_r p & \omega_r L_r \\ -\omega_r M & Mp & -\omega_r L_r & r_r + L_r p \end{bmatrix} \begin{bmatrix} i_{s\alpha} \\ i_{s\beta} \\ i_{r\alpha} \\ i_{r\beta} \end{bmatrix}$$
(1)

With: $L_s = L_{ls} + M$, $L_r = L_{lr} + M$, $M = 3L_{ms}$

This model is similar to the three phase machine model in the stationary reference frame.

Machine model in z1-z2 subspace

$$\begin{bmatrix} v_{sz1} \\ v_{sz2} \end{bmatrix} = \begin{bmatrix} r_s + L_{ls}p & 0 \\ 0 & r_s + L_{ls}p \end{bmatrix} \cdot \begin{bmatrix} i_{sz1} \\ i_{sz2} \end{bmatrix}$$
 (2a)

$$\begin{bmatrix} 0 \\ 0 \end{bmatrix} = \begin{bmatrix} r_r + L_{lr}p & 0 \\ 0 & r_r + L_{lr}p \end{bmatrix} \cdot \begin{bmatrix} i_{rz1} \\ i_{rz2} \end{bmatrix}$$
 (2b)

Machine model in z3-z4 subspace

$$\begin{bmatrix} v_{sz3} \\ v_{sz4} \end{bmatrix} = \begin{bmatrix} r_s + L_{ls}p & 0 \\ 0 & r_s + L_{ls}p \end{bmatrix} \cdot \begin{bmatrix} i_{sz3} \\ i_{sz4} \end{bmatrix}$$
(3a)

$$\begin{bmatrix} 0 \\ 0 \end{bmatrix} = \begin{bmatrix} r_s + L_{ls}p & 0 \\ 0 & r_s + L_{ls}p \end{bmatrix} \begin{bmatrix} i_{rz3} \\ i_{rz4} \end{bmatrix}$$
 (3b)

As can be seen from these three subsystems, the electromechanical energy conversion takes place only in α - β subsystem, and the other subsystems do not make any contribution in the energy conversion. The z1-z2 and z3-z4 subsystems generate the only losses that should be controlled to be minimized. It can be concluded that the torque and speed controller structure and analysis for SPIM are almost the same as those for three-phase induction machines. Therefore, we use the equivalent model in α - β subspace.

2-2- Model in the open phase fault condition

The model of SPIM under the opening phase 1 condition is presented in [3] (see Figure 2).

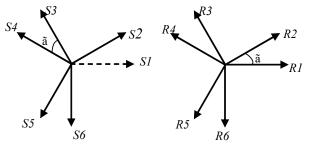


Figure 2. Stator and rotor winding axes (s1 is opened).

As shown in Figure 2, the SPIM machine is a fivedimensional system in the stator when one of the stator's phases is opened. Meanwhile, the rotor will be modeled as a six-dimensional system. The block-decoupled model of SPIM in $\alpha 1$ - $\beta 1$ and z 1-z 2-z 3 subspaces are as follows:

 $\alpha 1$ - $\beta 1$ subspace: The stator and rotor voltage equations for this subsystem are given by

$$\begin{cases} v_{s\alpha 1} = R_s \, i_{s\alpha 1} + \frac{d}{dt} \psi_{s\alpha 1} \\ v_{s\beta 1} = R_s \, i_{s\beta 1} + \frac{d}{dt} \psi_{s\beta 1} \end{cases}$$
(4a)

$$\begin{cases}
0 = R_r . i_{r\alpha 1} + \frac{d}{dt} \psi_{r\alpha 1} + \omega_r . \psi_{r\beta 1} \\
0 = R_r . i_{r\beta 1} + \frac{d}{dt} \psi_{r\beta 1} - \omega_r . \psi_{r\alpha 1}
\end{cases}$$
(4b)

where R_s and R_r are the stator and rotor resistances. The variables $\psi_s \alpha 1$, $\psi_s \beta 1$, $\psi_r \alpha 1$ and $\psi_r \beta 1$ are $\alpha_1 - \beta_1$ components the stator and the rotor fluxes and are described as follows:

$$\begin{cases} \psi_{s\alpha 1} = L_{sd} i_{s\alpha 1} + M_{d} i_{r\alpha 1} \\ \psi_{s\beta 1} = L_{sq} i_{s\beta 1} + M_{q} i_{r\beta 1} \end{cases}$$
 (5)

$$\begin{cases} \psi_{r\alpha 1} = M_d i_{s\alpha 1} + L_r i_{r\alpha 1} \\ \psi_{r\beta 1} = M_q i_{s\beta 1} + L_r i_{r\beta 1} \end{cases}$$
 (6)

where L_r is the rotor inductance and ω_r is the rotor angular speed. Table 10 gives Lsd, Lsq, Md and Mq for all cases up to three open phases (N = 5, 4 and 3). It can be noticed that the SPIM model in α - β subspace is always the same as that in (1), whatever the open phases are.

z1-z2-z3 subspace: The stator voltage equations are:

$$\begin{cases} v_{sz1} = R_s \, i_{sz1} + L_{ls} \, \frac{di_{sz1}}{dt} \\ v_{sz2} = R_s \, i_{sz2} + L_{ls} \, \frac{di_{sz2}}{dt} \\ v_{sz3} = R_s \, i_{sz3} + L_{ls} \, \frac{di_{sz3}}{dt} \end{cases}$$
(7)

It can be concluded from (3) and (7) that only the z subspace is related to the losses. Therefore, a suitable control strategy is required to minimize the z1-z2-z3 currents.

Torque Expression Under Open Phase Fault Conditions It is known that the electromagnetic torque oscillates with a faulty open phase. Torque response in the faulty mode operation is as follows [3]:

$$\Gamma_{\rm m} = \frac{p}{L_r} \left(M_q i_{s\beta 1} \psi_{r\alpha 1} - M_d i_{s\alpha 1} \psi_{r\beta 1} \right) = \Gamma_{mean} + \Gamma_{oscil}$$
 (8a)

$$\Gamma_{mean} = \frac{p}{L_r} \frac{1}{D} \left[M_d M_q I_{\alpha} I_{\beta} \sqrt{1 + \tau_r^2 \omega_s^2} \cdot \sin(\varphi_1 - \varphi_2) - \frac{\tau_r \omega_r}{2} \left(M_d^2 I_{\alpha}^2 + M_q^2 I_{\beta}^2 \right) \cdot \cos(\varphi_1) \right]$$
(8b)

$$\Gamma_{oscil} = \frac{p}{L_r} \frac{\tau_r \omega_r}{2D} \left(M_d^2 I_\alpha^2 - M_q^2 I_\beta^2 \right) \cdot \cos \left(2\theta_s - \varphi_1 \right)$$
 (8c)

with
$$\varphi_1 = \tan^{-1}\left(\frac{2\tau_r\omega_s}{1+\tau_r^2(\omega_r^2-\omega_s^2)}\right)$$
, $\varphi_2 = \tan^{-1}\left(\tau_r\omega_s\right)$ and
$$D = \sqrt{\left[1+\tau_r^2(\omega_r^2-\omega_s^2)\right]^2+4\tau_r^2\omega_s^2}$$

Equation (8) shows that in the case of open phase fault, the electromagnetic torque may be decomposed into two components, namely an average component and the other one oscillating at twice the excitation frequency θ_s (second harmonic).

In the open phase fault conditions, the dynamical properties of the machine will change from its balanced operating conditions, and field-oriented control strategies or direct torque control methods developed for a balanced winding structure will no longer work correctly. In what follows, DTC of SPIM under the condition of open phase fault is investigated.

3- PROPOSED DTC METHOD

3- 1- DTC in the normal conditions

In [12], the DTC of SPIM in the normal mode has been described. The phase voltages of SPIM with respect to its neutrals are as follows:

$$\begin{cases} Valn = 1/3* [2*Valo - Vblo - Vclo] \\ Vbln = 1/3* [2*Vblo - Valo - Vclo] \\ Vcln = 1/3* [2*Vclo - Vblo - Valo] \\ Va2n = 1/3* [2*Va2o - Vb2o - Vc2o] \\ Vb2n = 1/3* [2*Vb2o - Va2o - Vc2o] \\ Vc2n = 1/3* [2*Vc2o - Vb2o - Va2o] \\ \end{cases}$$
(9)

By combinational analysis of all states of 12 inverter keys, a total of 64 switching modes are obtained. By applying the proper transformation, 64 voltage vectors are projected on the α - β , z1-z2 and z3-z4 subspaces. Figure 3 shows the selected space voltage vectors on the α - β plane for the SPIM.

The decimal numbers in the Figure 3 show switching states of the inverter switches. By converting each decimal number to a six digit binary number, the 1's indicate the state of the upper switch in the corresponding arm of the inverter. The most significant bit (MSB) of the number represents the switching state of phase a1, the second MSB for the phase a2, the third for phase b1, and so on. Thus, by selecting the space voltage vector according to Table 1, the stator flux and electromagnetic torque of machine can be controlled [12].

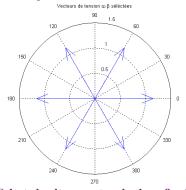


Fig. 3. Selected voltage vectors in the α - β subspace.

Table 1: Stator flux and electric torque control for SPIM

Sec	ctor	1	2	2			
$U\lambda_{\scriptscriptstyle s}$	UT_{e}	1	2	3	4	5	6
1	1	56	28	14	7	35	49
1	0	0	0	0	0	0	0
1	-1	35	49	56	28	14	7
0	1	28	14	7	35	49	56
0	0	63	0	0	0	0	0
0	-1	7	35	49	56	28	14

3- 2- Analyzing DTC in the open phase fault condition In this section, the DTC of SPIM under the condition of opening one or more phases is investigated. In the open phase fault, the neutrals of the machine will be connected to each other and the configuration of machine changes to one common neutral. In the open phase 1, the phase voltages of the machine with respect to its neutral will be written as follows:

$$\begin{cases} Vb1n = 1/5*[4*Vb1o-Vc1o-Va2o-Vb2o-Vc2o] \\ Vc1n = 1/5*[-Vb1o+4*Vc1o-Va2o-Vb2o-Vc2o] \\ Va2n = 1/5*[-Vb1o-Vc1o+4*Va2o-Vb2o-Vc2o] \\ Vb2n = 1/5*[-Vb1o-Vc1o-Va2o+4*Vb2o-Vc2o] \\ Vc2n = 1/5*[-Vb1o-Vc1o-Va2o-Vb2o+4*Vc2o] \end{cases}$$

In this case, a total of 32 switching modes can be obtained. By applying a proper five-dimensional transformation, 32 voltage vectors on the α , β , z1, z2, and z3 coordinates will be obtained. Table 2 shows the projected space voltage vectors on the α , β , z1, z2, and z3 coordinates.

From Table 2, one cannot find any α - β projected component with corresponding zero components on the z1, z2, and z3 axes. Each selected space voltage vectors produces high power losses due to non-zero projection on the z1, z2, and z3 axis.

To study more open phase conditions and apply DTC, the projection of space voltage vectors on the decoupled spaces by a proper transformation matrix is needed.

Opening one phase (phase 1): In this case, SPIM model is transformed to an asymmetrical five-phase machine. The projected space voltage vectors (SVV) on a five-dimensional decoupled space is shown in Table 2.

Opening two phases: In this case, one may recognize three different opening phase configurations, which are opening phases 1 and 2 (phases 1, 2), opening phases 1 and 3 (phases 1, 3), and opening phases 1 and 4 (phases 1, 4).

In all three cases, SPIM is transformed to an asymmetrical four-phase machine. The projected space voltage vectors on a four-dimensional decoupled space are shown in Tables 3-5. **Opening three phases:** In this case, one may recognize three different configurations for opened phases, that are phases 123, phases 124, and phases 135. In the first and second case, SPIM transforms to an Asymmetrical three-phase machine, and in the opening phases 135, the SPIM transforms to a symmetrical three-phase machine. The projected space voltage vectors to a three dimensional decoupled space are shown in Tables 6 to 8. It seems from Tables 3 to 7, for every non-zero projection on the α and β axes, one may not find zero or near zero components on the z-axis. In this case, the root mean square (rms) of total z-axis component voltages is introduced as a norm for

comparing different switching states of SPIM in the view point of losses under open phase fault conditions. Tables 11 to 13 give rms values of total z-axis component voltages in the case of opening phase 1, phases 1 and 2, phases 1 and 3, and phases 1 and 4.

As can be seen, the minimum harmonic voltage in the case of opening phase 1 is 13.47 V, in the case of opening phases 1& 2 is 11.1243 V, in the case of opening phases 1 & 3 is 17.5710 V, and in the case of opening phases 1 & 4 is 11.1155 V. Only in the case of opening three phases with 120 electrical degrees (opening phases 135), can we find a symmetrical three-phase system with zero total harmonic voltage. On the other hand, except for open phase condition 135, DTC cannot control the machine properly in the open phase fault conditions.

4- Test Results

In order to investigate DTC for controlling SPIM due to an opened stator phase fault, an experimental test-rig bed is developed (Fig. 4). The experimental setup is composed of a low power SPIM supplied by two three-phase voltage source inverters whose DC link voltage is fixed at 42 V. The switching frequency is imposed at 5 kHz using the classical sampled natural PWM technique generated by a FPGA. This board receives the stator current data through six 12bit A/D converters. An electromagnetic power brake stiffly connected to the SPIM rotor shaft is used to generate the load torque. The speed is measured through a 4096-points encoder. The SPIM drive main parameters are given in Table 9. In order to open phase s1, the corresponding VSI winding connection is removed. Figure 5 shows the block diagram of the DTC technique. We use inverse DTC method addressed in [13]. Fig. 6 shows experimental results for DTC method in the normal condition, while Fig. 7 shows experimental results for DTC method in the fault condition (phase s1 open). As can be seen from Fig. 7, low-frequency ripples appear on the angular speed, but its oscillations rate is very low thanks to the mechanical subsystem natural filtering. Fig. 8 illustrates experimental results for DTC method in the fault condition (phases s1, s3, and s5 are open). As can be observed from Fig. 8, the harmonic currents due to projected voltage vectors on the z-space are almost zero, because of zero voltage projection on the z-space in this case.

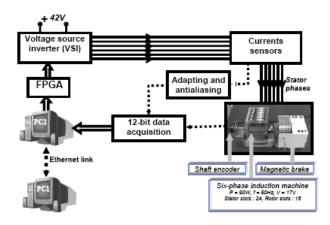


Fig. 4. Experimental test-rig.

Table 2. Projected SVV in the opening phase 1

No.	α	β	Z 1	Z2	Z3
0	0	0	0	0	0
1	4.85	-24.25	-1.52	-31.54	36.97
2	-7.27	-21.00	-11.29	35.56	-35.78
3	-2.42	-45.25	-12.81	4.02	1.18
4	-16.15	12.12	40.74	-26.44	-16.12
5	-11.30	-12.12	39.22	-57.98	20.85
6	-23.42	-8.87	29.46	9.12	-51.90
7	-18.57	-33.12	27.93	-22.42	-14.93
8	-7.27	21.00	-48.36	3.46	17.95
9	-2.42	-3.25	-49.88	-28.08	54.92
10	-14.55	0.00	-59.64	39.02	-17.83
11	-9.70	-24.25	-61.16	7.48	19.13
12	-23.42	33.12	-7.61	-22.98	1.83
13	-18.57	8.88	-9.13	-54.52	38.8
14	-30.70	12.12	-18.90	12.58	-33.95
15	-25.85	-12.12	-20.42	-18.96	3.01
16	25.85	12.12	20.42	18.96	-3.01
17	30.70	-12.12	18.90	-12.58	33.95
18	18.57	-8.88	9.13	54.52	-38. 8
19	23.42	-33.12	7.61	22.98	-1.83
20	9.70	24.25	61.16	-7.48	-19.13
21	14.55	-0.00	59.64	-39.02	17.83
22	2.42	3.25	49.88	28.08	-54.92
23	7.27	-21.00	48.36	-3.46	-17.95
24	18.57	33.12	-27.93	22.42	14.94
25	23.42	8.87	-29.46	-9.12	51.90
26	11.30	12.12	-39.22	57.98	-20.85
27	16.15	-12.12	-40.74	26.44	16.12
28	2.42	45.25	12.81	-4.02	-1.18
29	7.27	21.00	11.29	-35.56	35.78
30	-4.85	24.25	1.52	31.54	-36.97
31	0	0	0	0	0

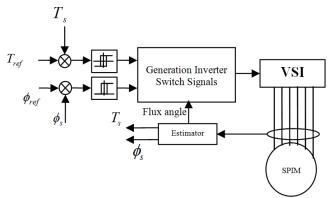


Fig. 5. Block diagram of DTC system.

Table 3. Projected space voltage vector in the opening phase 1 and 2

		1 and 2	•	
No.	α	β	Z1	Z2
0	0	0	0	0
1	11.31	-21.22	-31.28	32.14
2	-0.81	-17.97	42.40	-31.83
3	10.50	-39.19	11.12	0.31
4	-9.69	15.15	-40.58	-34.13
5	1.62	-6.06	-71.86	-1.99
6	-10.50	-2.81	1.82	-65.96
7	0.81	-24.03	-29.46	-33.82
8	-0.81	24.03	29.46	33.82
9	10.50	2.81	-1.82	65.96
10	-1.62	6.06	71.86	1.99
11	9.69	-15.15	40.58	34.13
12	-10.50	39.19	-11.12	-0.31
13	0.81	17.97	-42.40	31.83
14	-11.31	21.22	31.28	-32.14
15	0	0	0	0

Table 4. Projected space voltage vector in the opening phases 1 and 3

		1 anu	<i>5</i>	
No.	α	β	Z1	Z2
0	0	0	0	0
1	3.03	-19	-39.43	27.00
2	-9.09	-15.75	27.61	-44.90
3	-6.06	-34.75	-11.82	-17.90
4	-17.97	17.37	-9.20	14.97
5	-14.94	-1.62	-48.63	41.97
6	-27.06	1.62	18.40	-29.93
7	-24.03	-17.37	-21.02	-2.93
8	24.03	17.37	21.02	2.93
9	27.06	-1.62	-18.40	29.93
10	14.94	1.62	48.63	-41.97
11	17.97	-17.37	9.20	-14.97
12	6.06	34.74	11.82	17.90
13	9.09	15.75	-27.61	44.90
14	-3.03	19	39.43	-27.00
15	0	0	0	0

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5- CONCLUSION

In this paper, the direct torque control of a six-phase induction motor, under open phase fault conditions was investigated. At first, it was shown that the suppression of one stator phase produces the second harmonic ripples on the motor torque whose amplitude is proportional to the difference between

Table 5. Projected space voltage vector in the opening phases 1 and 4

No. α β Z1 Z2 0 0 0 0 0 1 0.81 -21.22 -37.01 31.53 2 -11.31 -17.97 28.88 -39.12 3 -10.50 -39.19 -8.13 -7.58 4 -11.31 24.03 -7.99 16.72 5 -10.50 2.81 -45.01 48.26 6 -22.62 6.06 20.89 -22.39 7 -21.81 -15.15 -16.13 9.14 8 21.81 15.15 16.13 -9.14 9 22.62 -6.06 -20.89 22.39 10 10.50 -2.81 45.01 -48.25 11 11.31 -24.03 7.99 -16.72 12 10.50 39.19 8.13 7.58 13 11.31 17.97 -28.88 39.12 14 -0.81 21.22 37.01			1 and -	•	
1 0.81 -21.22 -37.01 31.53 2 -11.31 -17.97 28.88 -39.12 3 -10.50 -39.19 -8.13 -7.58 4 -11.31 24.03 -7.99 16.72 5 -10.50 2.81 -45.01 48.26 6 -22.62 6.06 20.89 -22.39 7 -21.81 -15.15 -16.13 9.14 8 21.81 15.15 16.13 -9.14 9 22.62 -6.06 -20.89 22.39 10 10.50 -2.81 45.01 -48.25 11 11.31 -24.03 7.99 -16.72 12 10.50 39.19 8.13 7.58 13 11.31 17.97 -28.88 39.12 14 -0.81 21.22 37.01 -31.53	No.	α	β	Z1	Z2
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3 -10.50 -39.19 -8.13 -7.58 4 -11.31 24.03 -7.99 16.72 5 -10.50 2.81 -45.01 48.26 6 -22.62 6.06 20.89 -22.39 7 -21.81 -15.15 -16.13 9.14 8 21.81 15.15 16.13 -9.14 9 22.62 -6.06 -20.89 22.39 10 10.50 -2.81 45.01 -48.25 11 11.31 -24.03 7.99 -16.72 12 10.50 39.19 8.13 7.58 13 11.31 17.97 -28.88 39.12 14 -0.81 21.22 37.01 -31.53	1	0.81	-21.22	-37.01	31.53
4 -11.31 24.03 -7.99 16.72 5 -10.50 2.81 -45.01 48.26 6 -22.62 6.06 20.89 -22.39 7 -21.81 -15.15 -16.13 9.14 8 21.81 15.15 16.13 -9.14 9 22.62 -6.06 -20.89 22.39 10 10.50 -2.81 45.01 -48.25 11 11.31 -24.03 7.99 -16.72 12 10.50 39.19 8.13 7.58 13 11.31 17.97 -28.88 39.12 14 -0.81 21.22 37.01 -31.53	2	-11.31	-17.97	28.88	-39.12
5 -10.50 2.81 -45.01 48.26 6 -22.62 6.06 20.89 -22.39 7 -21.81 -15.15 -16.13 9.14 8 21.81 15.15 16.13 -9.14 9 22.62 -6.06 -20.89 22.39 10 10.50 -2.81 45.01 -48.25 11 11.31 -24.03 7.99 -16.72 12 10.50 39.19 8.13 7.58 13 11.31 17.97 -28.88 39.12 14 -0.81 21.22 37.01 -31.53	3	-10.50	-39.19	-8.13	-7.58
6 -22.62 6.06 20.89 -22.39 7 -21.81 -15.15 -16.13 9.14 8 21.81 15.15 16.13 -9.14 9 22.62 -6.06 -20.89 22.39 10 10.50 -2.81 45.01 -48.25 11 11.31 -24.03 7.99 -16.72 12 10.50 39.19 8.13 7.58 13 11.31 17.97 -28.88 39.12 14 -0.81 21.22 37.01 -31.53	4	-11.31	24.03	-7.99	16.72
7 -21.81 -15.15 -16.13 9.14 8 21.81 15.15 16.13 -9.14 9 22.62 -6.06 -20.89 22.39 10 10.50 -2.81 45.01 -48.25 11 11.31 -24.03 7.99 -16.72 12 10.50 39.19 8.13 7.58 13 11.31 17.97 -28.88 39.12 14 -0.81 21.22 37.01 -31.53	5	-10.50	2.81	-45.01	48.26
8 21.81 15.15 16.13 -9.14 9 22.62 -6.06 -20.89 22.39 10 10.50 -2.81 45.01 -48.25 11 11.31 -24.03 7.99 -16.72 12 10.50 39.19 8.13 7.58 13 11.31 17.97 -28.88 39.12 14 -0.81 21.22 37.01 -31.53	6	-22.62	6.06	20.89	-22.39
9 22.62 -6.06 -20.89 22.39 10 10.50 -2.81 45.01 -48.25 11 11.31 -24.03 7.99 -16.72 12 10.50 39.19 8.13 7.58 13 11.31 17.97 -28.88 39.12 14 -0.81 21.22 37.01 -31.53	7	-21.81	-15.15	-16.13	9.14
10 10.50 -2.81 45.01 -48.25 11 11.31 -24.03 7.99 -16.72 12 10.50 39.19 8.13 7.58 13 11.31 17.97 -28.88 39.12 14 -0.81 21.22 37.01 -31.53	8	21.81	15.15	16.13	-9.14
11 11.31 -24.03 7.99 -16.72 12 10.50 39.19 8.13 7.58 13 11.31 17.97 -28.88 39.12 14 -0.81 21.22 37.01 -31.53	9	22.62	-6.06	-20.89	22.39
12 10.50 39.19 8.13 7.58 13 11.31 17.97 -28.88 39.12 14 -0.81 21.22 37.01 -31.53	10	10.50	-2.81	45.01	-48.25
13 11.31 17.97 -28.88 39.12 14 -0.81 21.22 37.01 -31.53	11	11.31	-24.03	7.99	-16.72
14 -0.81 21.22 37.01 -31.53	12	10.50	39.19	8.13	7.58
	13	11.31	17.97	-28.88	39.12
15 0 0 0 0	14	-0.81	21.22	37.01	-31.53
	15	0	0	0	0

Table 6. Projected space voltage vector in the opening phases 1, 2 and 3

No.	α	β	Z1
0	0	0	0
1	11.04	-13.21	40.57
2	-1.08	-9.96	-55.42
3	9.96	-23.16	-14.85
4	-9.96	23.16	14.85
5	1.08	9.96	55.42
6	-11.04	13.21	-40.57
7	0	0	0

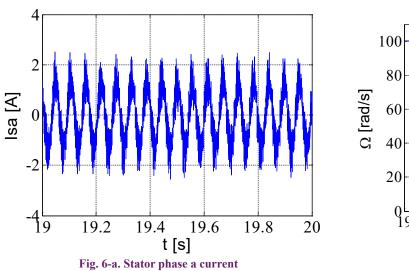
Table 7. Projected space voltage vector in the opening phases 1, 2 and 4

No.	α	β	Z1
0	0	0	0
1	8.08	-16.16	37.56
2	-4.04	-12.92	-51.32
3	4.04	-29.08	-13.75
4	-4.04	29.08	13.75
5	4.04	12.92	51.32
6	-8.08	16.16	-37.56
7	0	0	0

 α – β MMF components. Then, in order to control the SPIM under faulty conditions, we introduced projected space voltage vectors on the decoupled spaces by a proper transformation matrix. The results show that in the case of occurring a fault in an open phase, there is no space voltage vector with zero or near zero projection on the z_i axis. On the other hand, in the open phase fault conditions of SPIM, nonpulsating control by DTC is possible only in the case of opening a three-phase winding set. The test results show that the torque ripples were practically zero, opening a three-phase winding set.

Table 9. experimental setup parameters

Rated power	90 W
Rated torque	0.3 Nm
VSI DC bus voltage	42 V
Number of poles	2
Mutual inductance	30.9 mH
Stator resistance	$1.04~\Omega$
Stator leakage inductance	0.30 mH
Rotor resistance	$0.64~\Omega$
Rotor leakage inductance	0.65 mH
Friction coefficient	$4 \times 10^{-4} \text{ kg.m}^2/\text{s}$
Inertia	$9.5 \times 10^{-5} \text{ kg.m}^2$



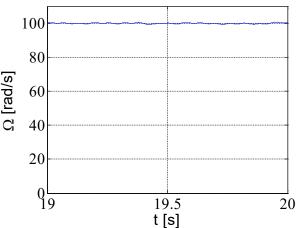
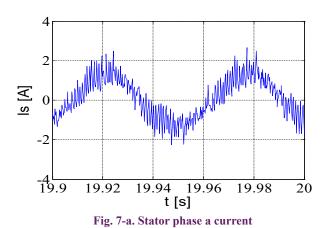


Fig. 6-b. Rotor speed (Ω)

Fig. 6. Experimental results, DTC in normal operation.



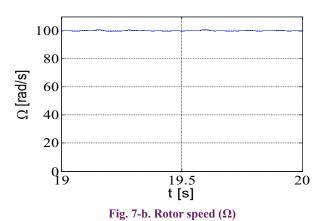


Fig. 7. Experimental results for open phase s1, DTC algorithm in non-compensated operation.

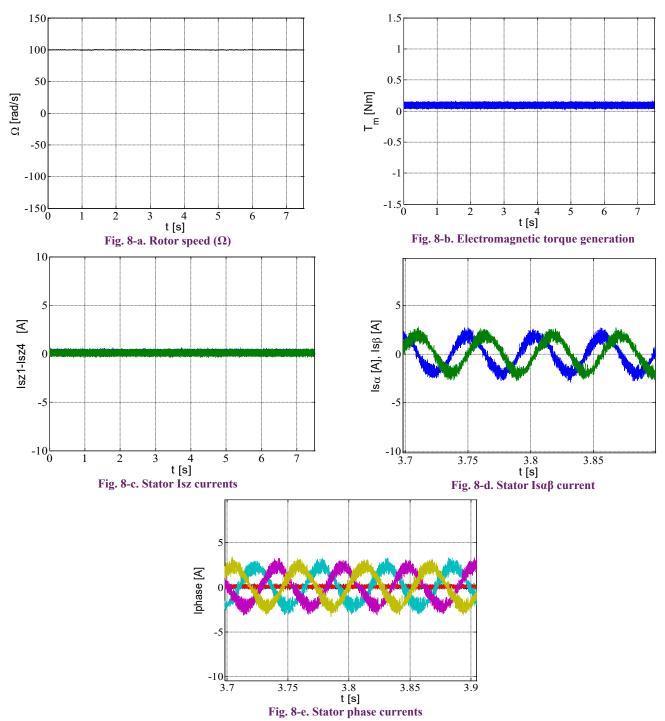


Fig. 8. Experimental results for s1, s3, and s5 open, DTC algorithm in non compensated operation

Table 10. Machine inductances with open phases

Open phase(s)	L_{sd}	L_{sq}	M_d	M_q
1;4	L _{ls} +2L _{ms}	$L_{ls}+3L_{ms}$	$2.449L_{ms}$	$3L_{ms}$
2;3;5;6	$L_{ls}+3L_{ms}$	L _{ls} +2L _{ms}	$3L_{ms}$	$2.449L_{ms}$
(1,2); (1,3); (1,5); (1,6) (2,4); (3,4); (4,5); (4,6)	$L_{ls}+1.5L_{ms}$	L _{ls} +2.5L _{ms}	$2.121L_{ms}$	2.739L _{ms}
(1,4)	$L_{ls}+L_{ms}$	L _{ls} +3L _{ms}	1.7321L _{ms}	$3L_{ms}$
(2,3); (2,6); (3,5); (5,6)	L _{ls} +2.5L _{ms}	L _{ls} +1.5L _{ms}	$2.739L_{ms}$	$2.121L_{\mathrm{ms}}$
(2,5); (3,6)	L _{ls} +3L _{ms}	$L_{ls}+1L_{ms}$	$3L_{ms}$	1.732L _{ms}
(1,2,3); $(1,2,6)$; $(2,3,4)$; $(3,4,5)$; $(4,5,6)$; $(1,3,5)$; $(1,5,6)$; $(2,4,6)$	$L_{ls}+1.5L_{ms}$	$L_{ls}+1.5L_{ms}$	2.121L _{ms}	$2.121L_{\mathrm{ms}}$
(1,2,4); $(1,2,5)$; $(1,3,4)$; $(3,4,6)$; $(1,3,6)$; $(1,4,5)$; $(1,4,6)$; $(2,4,5)$	L _{ls} +0.634L _{ms}	L _{ls} +2.366L _{ms}	1.3791L _{ms}	2.6642L _{ms}
(2,3,5); (2,3,6); (2,5,6); (3,5,6)	L _{ls} +2.366L _{ms}	L _{ls} +0.634L _{ms}	$2.6642L_{ms}$	1.3791L _{ms}

Table 11. Total rms components voltage in the case of opening phase 1

	ening phase i
No.	$V_{rmsz}1$
0	0
1	48.6196
2	51.6932
3	13.4777
4	51.1730
5	73.0384
6	60.3712
7	38.8027
8	51.6997
9	79.3266
10	73.4670
11	64.5171
12	24.2764
13	67.5369
14	40.8420
15	28.0271
16	28.0271
17	40.8420
18	67.5369
19	24.2764
20	64.5171
21	73.4670
22	79.3266
23	51.6997
24	38.8065
25	60.3712
26	73.0384
27	51.1730
28	13.4777
29	51.6932
30	48.6196
31	0

Table 12. Total rms components voltage in the case of opening phases 1&2

	phases reca				
No.	$V_{rmsz}12$				
0	0				
1	44.8488				
2	53.0180				
3	11.1243				
4	53.0245				
5	71.8875				
6	65.9851				
7	44.8518				
8	44.8518				
9	65.9851				
10	71.8875				
11	53.0245				
12	11.1243				
13	53.0180				
14	44.8488				
15	0				

Table 13.Total rms components voltage in the case of opening phases 1&3

No.	$V_{rmsz}13$
0	0
1	47.7883
2	52.7098
3	21.4505
4	17.5710
5	64.2367
6	35.1335
7	21.2232
8	21.2232
9	35.1335
10	64.2367
11	17.5710
12	21.4505
13	52.7098
14	47.7883
15	0

Table 14.Total rms components voltage in the case of opening phases 1&4

No.	$V_{rmsz}14$		
0	0		
1	48.6198		
2	48.6254		
3	11.1155		
4	18.5310		
5	65.9919		
6	30.6220		
7	18.5396		
8	18.5396		
9	30.6220		
10	65.9846		
11	18.5310		
12	11.1155		
13	48.6254		
14	48.6198		
15	0		

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